

# Modeling quasi-steady-state phase change transport in polymer electrolyte membrane fuel cells: *Effect of surface crack density*

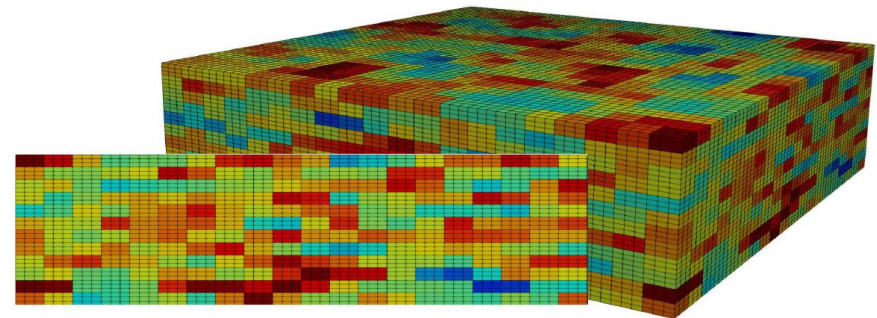
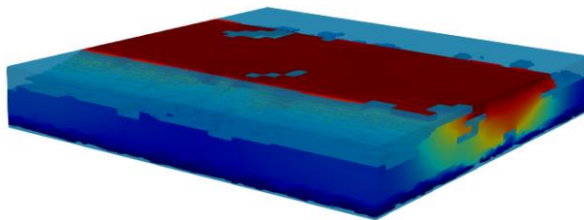
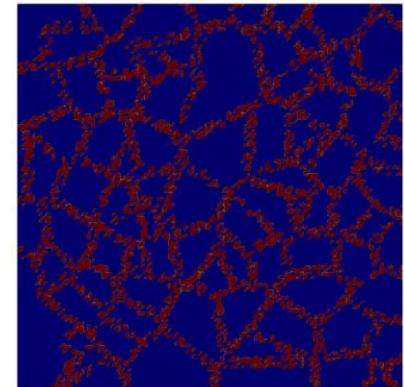
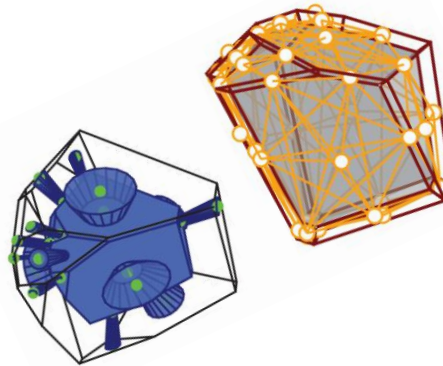
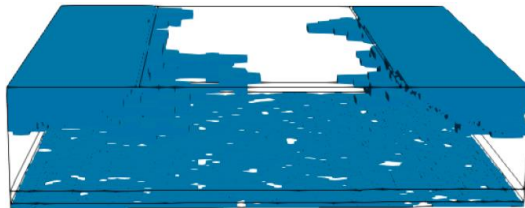
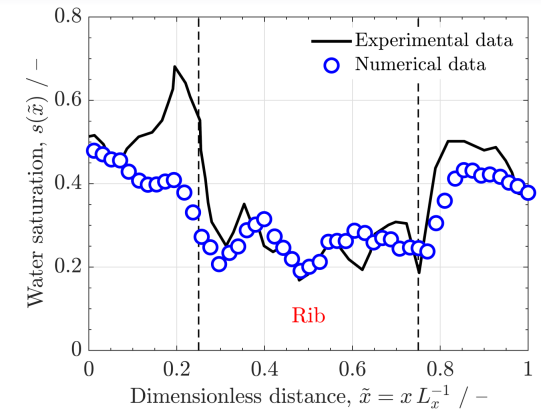
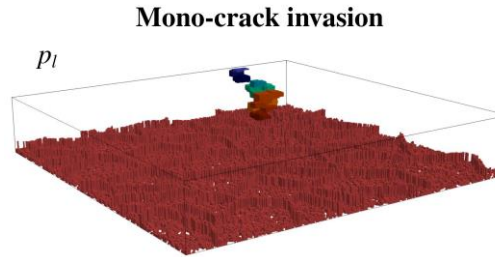
Pablo A. García-Salaberri

*Department of Thermal and Fluids Engineering  
University Carlos III of Madrid (Spain)*

**uc3m** *Fluid Mechanics*

# Outline

- Motivation
- Ex-situ invasion
- Quasi-steady-state phase change
- First insight on cracks
- Conclusions & future work

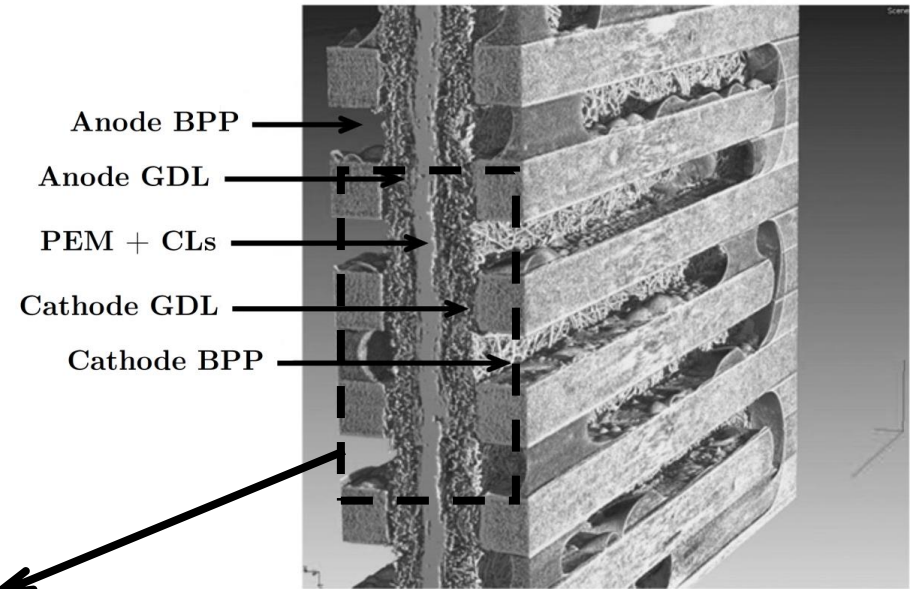
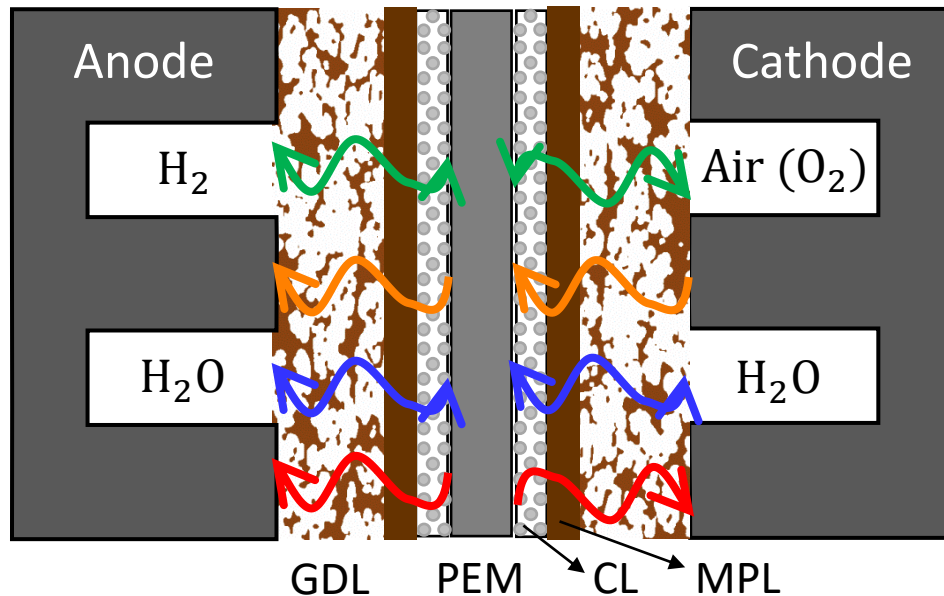


# Motivation I

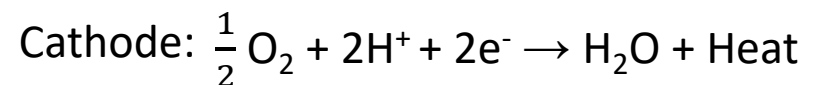
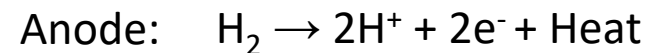
- **Layered Porous Media Assembly:** Understanding & Optimization
- **Multifunctional:** Coupled Phenomena

$$\delta_{\text{MEA}} \approx 150 - 450 \mu\text{m}$$

MEA



- 1) Gas species transport
- 2) Liquid water transport
- 3) Electron transport
- 4) Heat transport

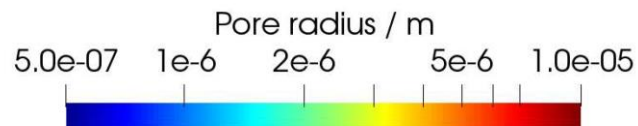
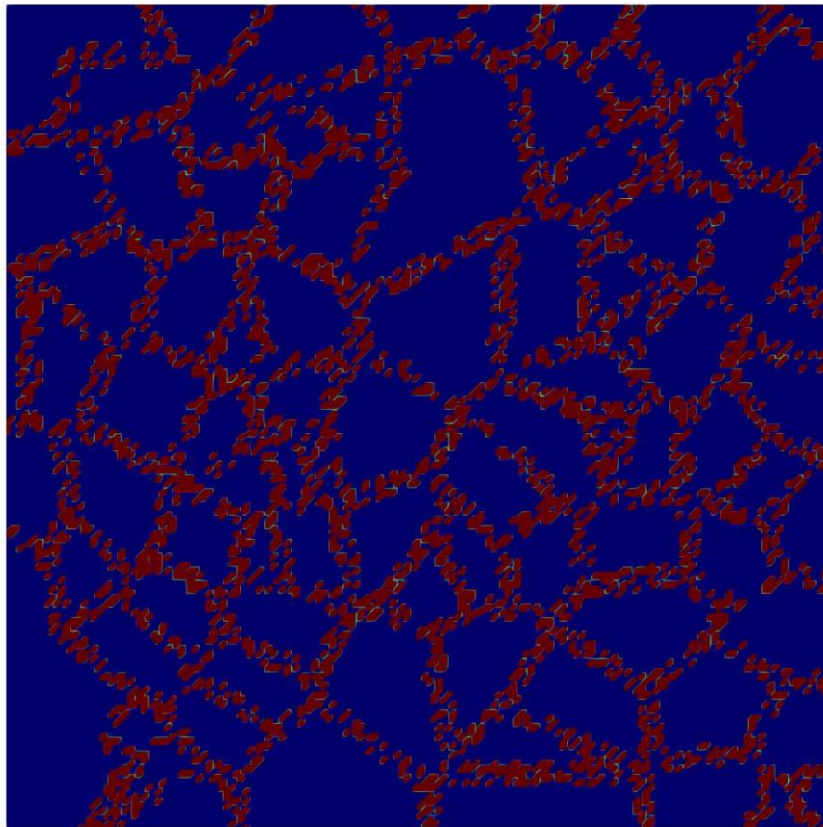




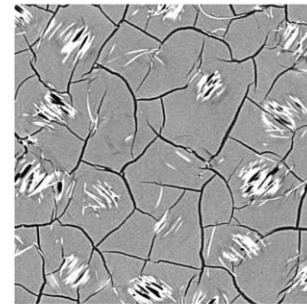
# Motivation II

*Journal of Power Sources*  
539 (2022) 231612.

- Cracks and defects



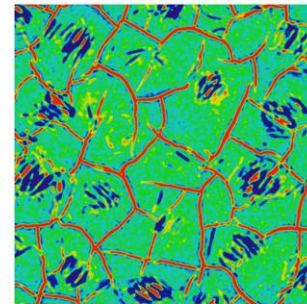
(a) W1S1009



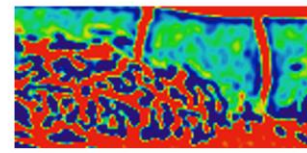
1 mm



0.25 mm

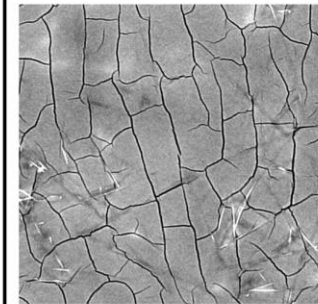


1 mm

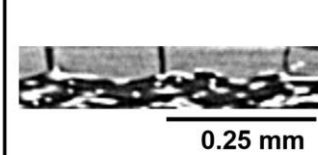


0.25 mm

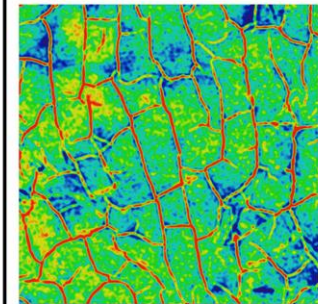
(b) GDL 120S



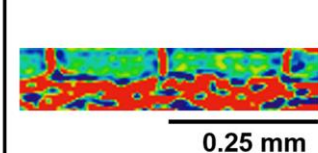
1 mm



0.25 mm

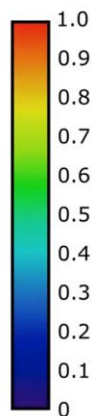


1 mm



0.25 mm

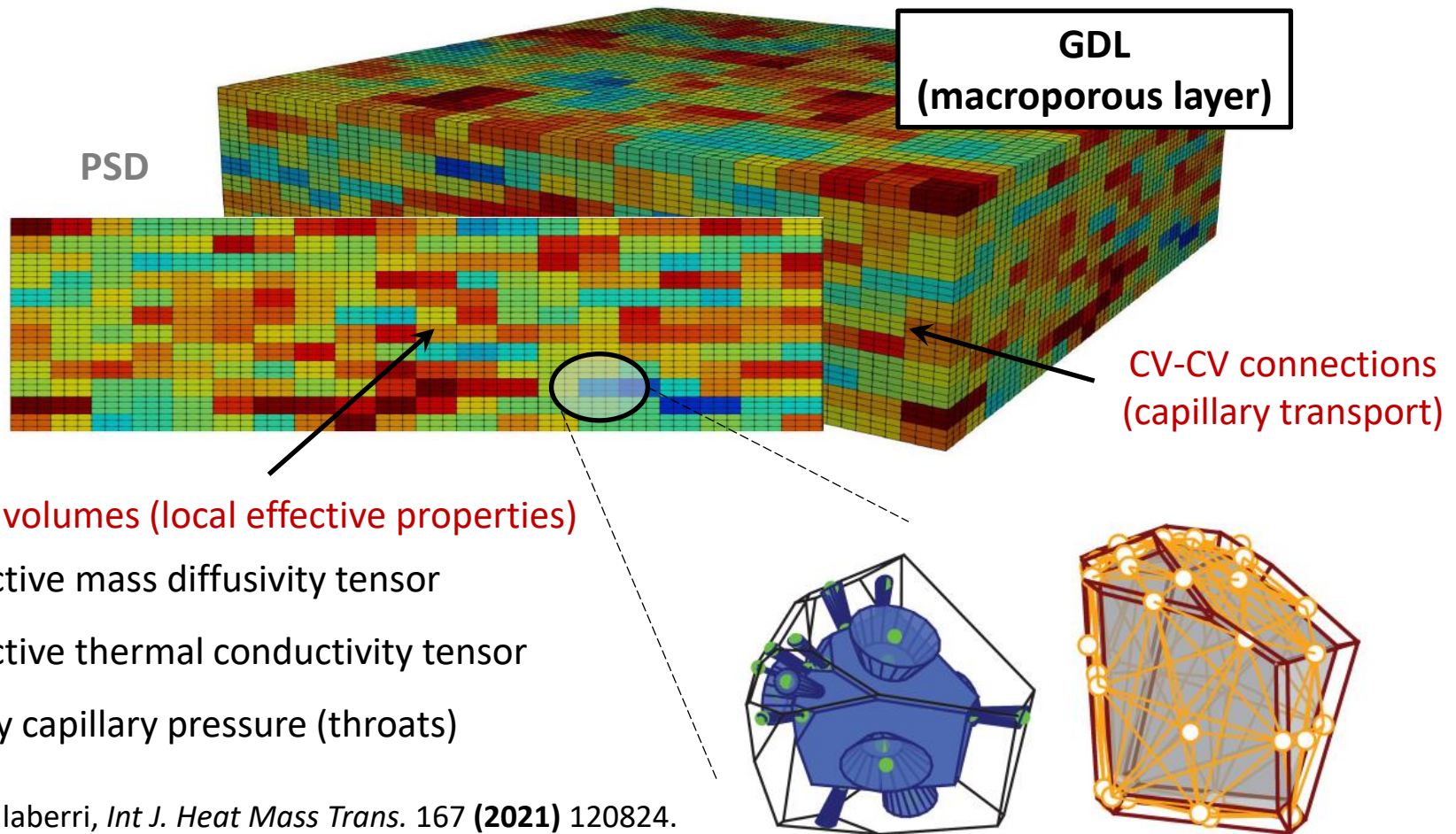
Porosity



Error

# Model Formulation

- **Highly Heterogeneous Thin Porous Media**
- **Hybrid Modeling:** Continuum Formulation + Discrete Formulation (based on Pore Network Modeling) for Liquid Water Transport



## Control volumes (local effective properties)

- Effective mass diffusivity tensor
- Effective thermal conductivity tensor
- Entry capillary pressure (throats)

García-Salaberri, *Int J. Heat Mass Trans.* 167 (2021) 120824.

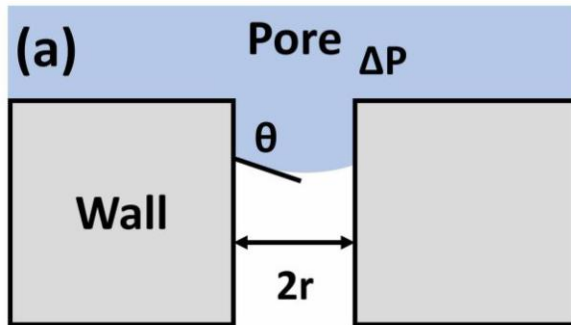
García-Salaberri, *J. Power Sources* (2023), in preparation.

# Local Entry Capillary Pressure

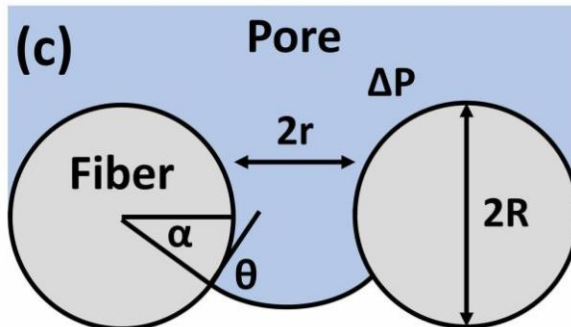
## MPL & CL (Cylindrical Pore)

$$p_c^{th} = \frac{-2\sigma}{r} \cos \theta$$

Washburn



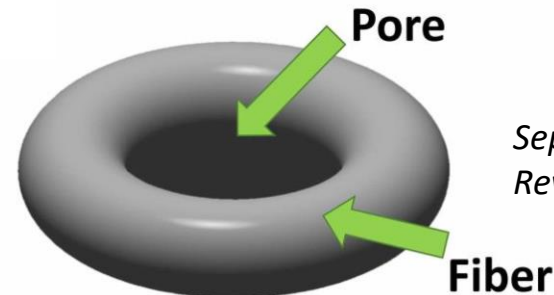
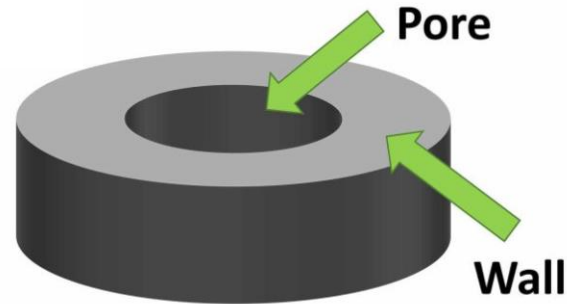
Purcell



## GDL (Toroidal Pore)

$$p_c^{th} = \frac{-2\sigma}{r_i} \frac{\cos(\theta - \alpha)}{1 + \frac{f_d}{2r} (1 - \cos \alpha)}$$

$$\alpha = \theta - \pi + \arcsin \left( \frac{\sin \theta}{1 + \frac{2r}{f_d}} \right)$$

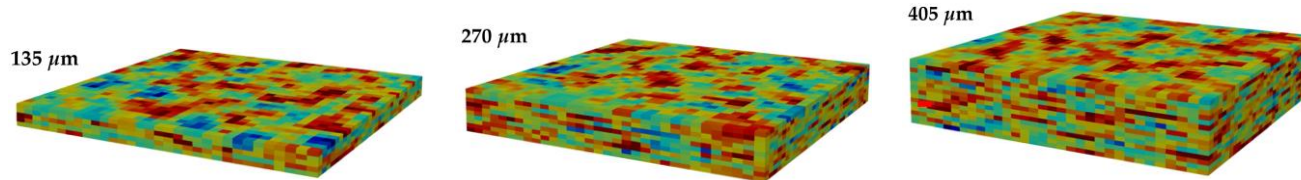


*Separation & Purification Reviews* 49 (2020) 317-356.

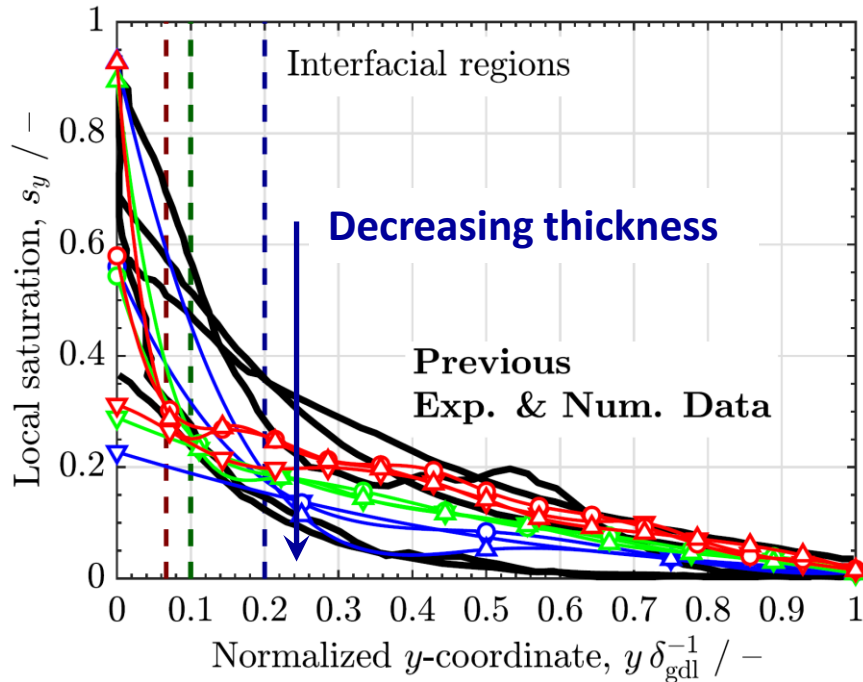


# Ex-situ Water Invasion: Thickness

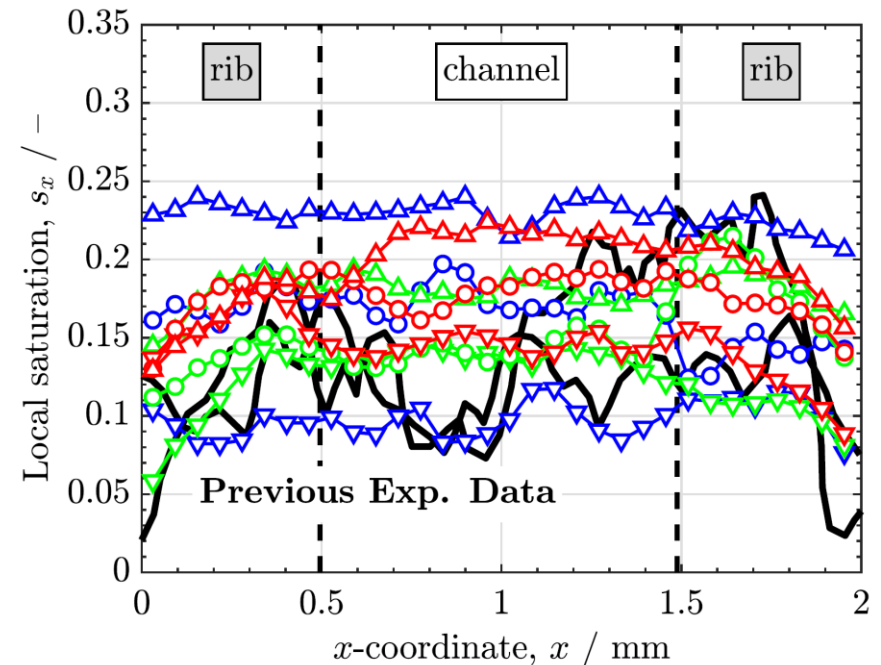
- Invasion-Percolation (no trapping):  $Ca \ll 1$



Through-Plane

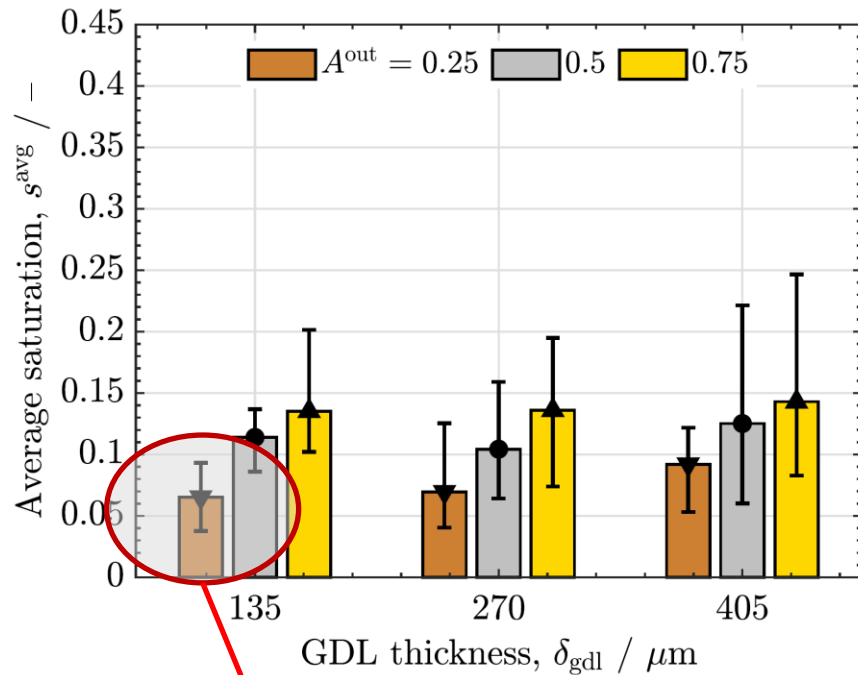


In-Plane

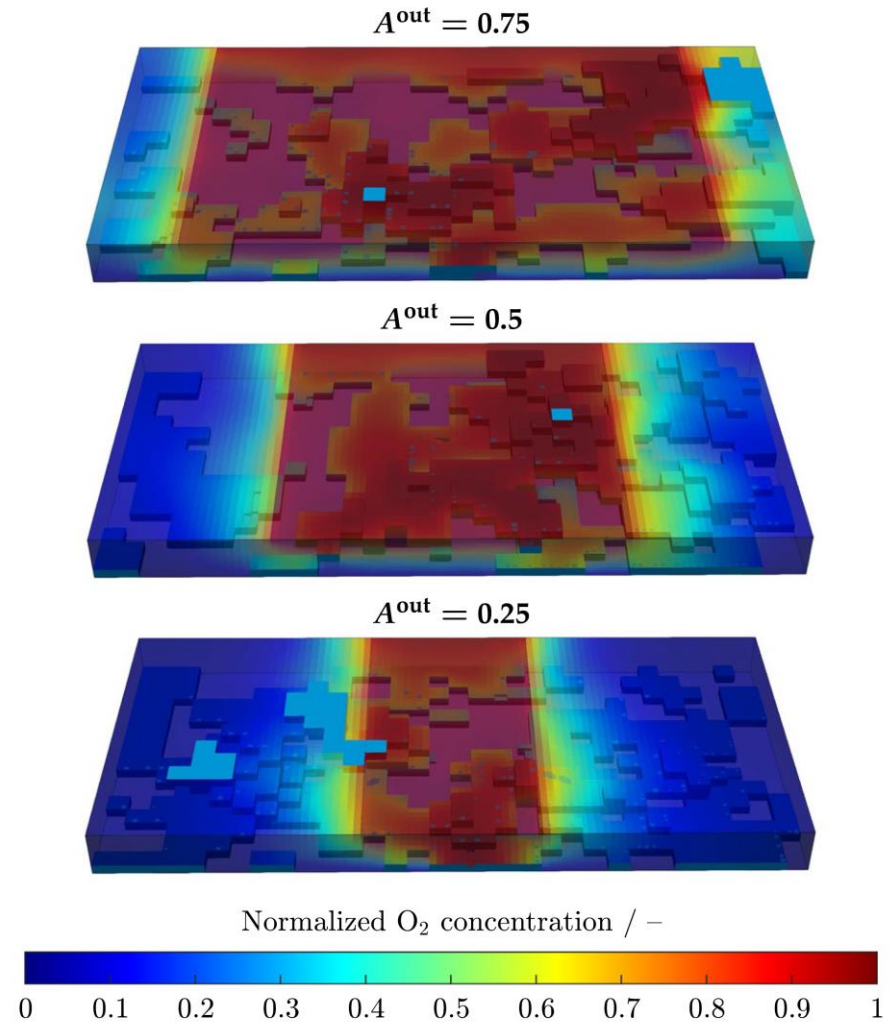


# Ex-situ Water Invasion: Outlet Area Fraction (OAF)

- Increasing outlet area fraction
- Decreasing thickness
- Facilitated water capillary transport



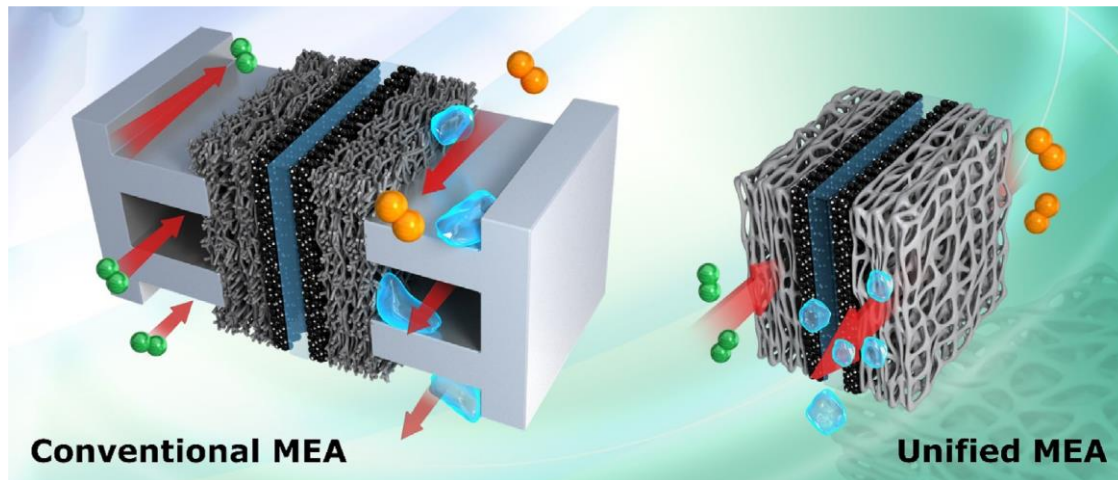
Small thickness, High OAF  
Reduced  $\text{O}_2$  transport resistance





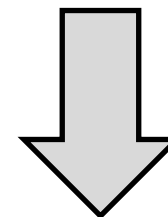
# Ex-situ Water Invasion: Porous Distributors

- Unified MEA/Flow distributor: Break-through volume power

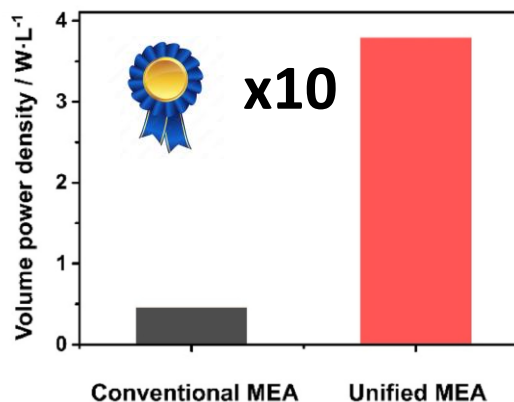
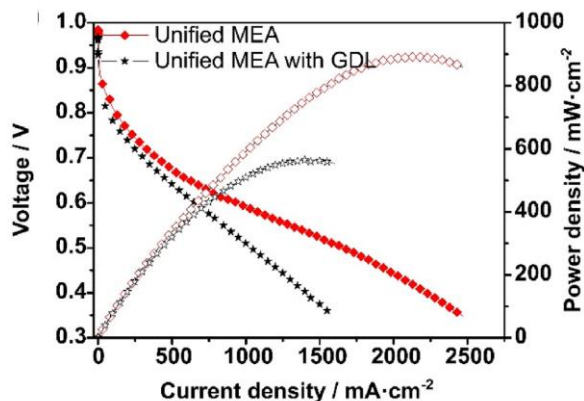


*Electrochimica Acta* 323  
(2019) 134808.

Small thickness, High OAF  
+  
Small rib width (fiber diameter)



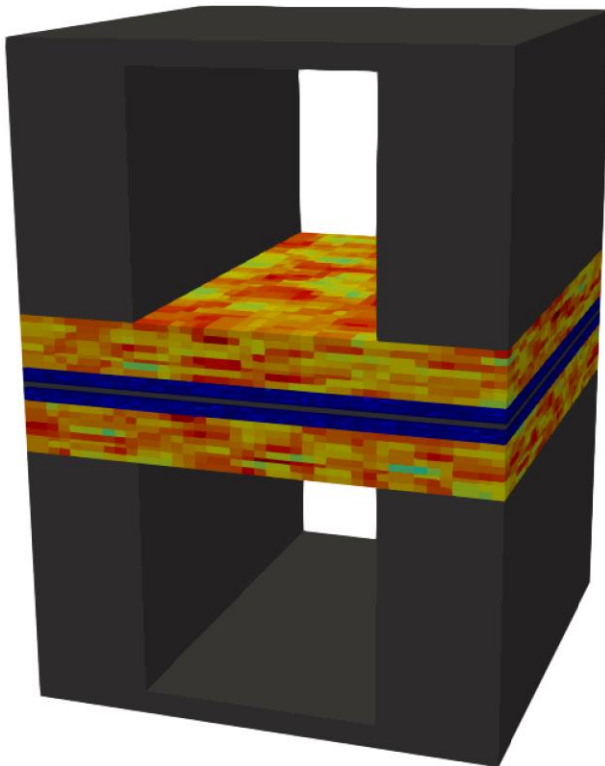
Unified Porous Assembly



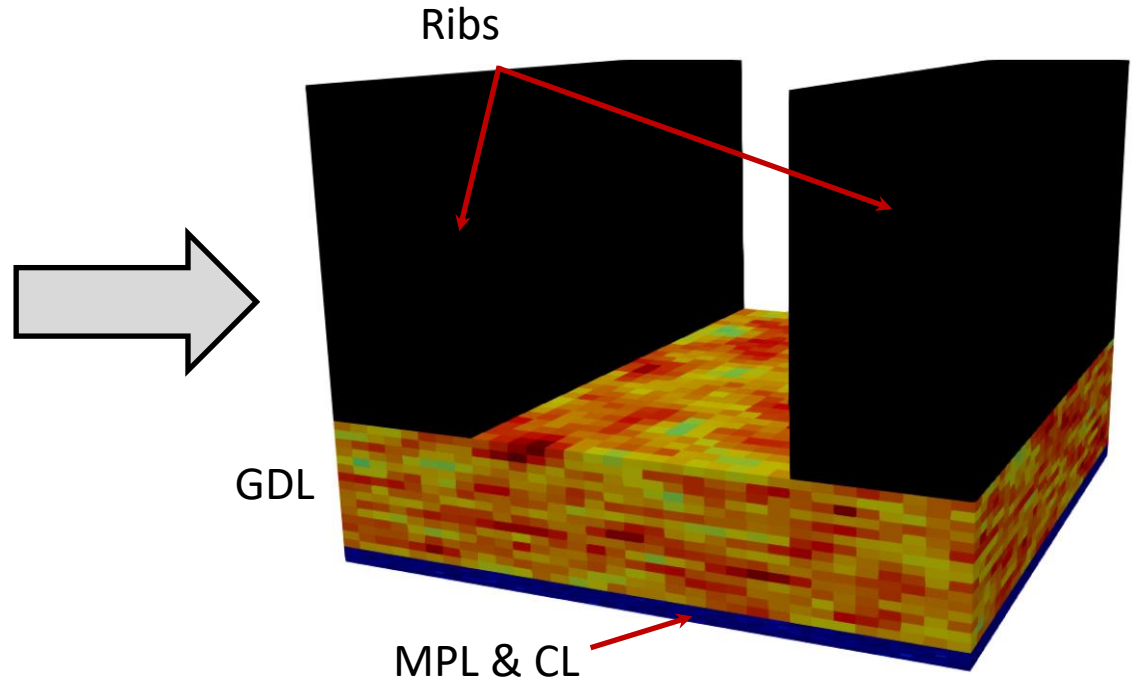
But...What about phase change of water?  
And cracks?

# Phase Change of Water: Still No Electrochemistry

Unit Cell



Half Cell



## Multiscale PSD

CL (0.001-0.1  $\mu\text{m}$ ), MPL (0.1-1  $\mu\text{m}$ ) & GDL (1-10  $\mu\text{m}$ )

# Quasi-Steady-State Assumption

## Nucleation + Growth Algorithm (Transport-Dominated Phase Change)

- Evaporation/Condensation interfacial kinetics is much faster than vapor diffusion & liquid-phase viscous capillary transport ( $t_{vl} \ll t_d \sim t_c$ )
- In agreement with previous experimental data & DNS

### Hertz–Knudsen Mass Transfer

$$t_{vl} \sim k_{vl}^{-1} \sim 10^{-7} - 10^{-6} \text{ s}$$

$$k_{vl} = A_{lv} \xi_{vl}; A_{vl} \sim 10^7 \text{ m}^{-1}, \xi_{vl} \sim 10^{-1} - 1 \text{ m s}^{-1}$$

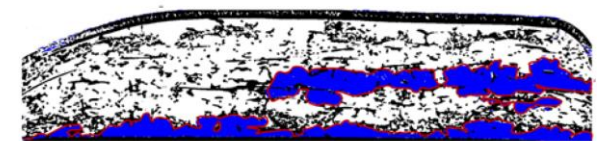
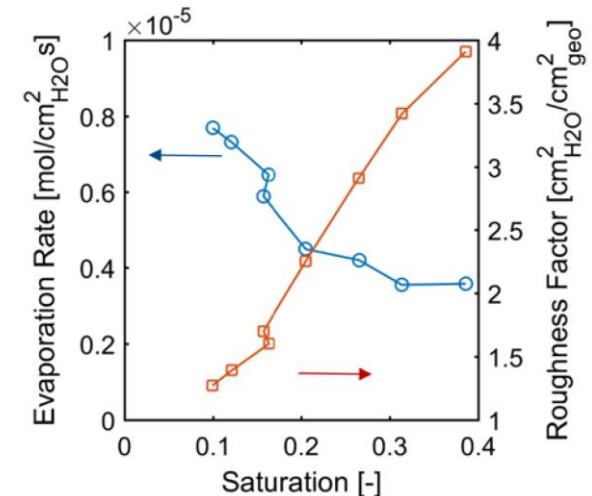
### Gas Diffusion & Capillary Transport

$$t_d \sim \frac{r_p^2}{D_{wv}^{eff}} \sim t_{cap} \sim \frac{\mu_w r_p^2}{K p_c^{th}} \sim 10^{-5} \text{ s}$$

*Int. J. Heat Mass Trans.* 129 (2019) 1250-1262.



*J. Phys. Chem. C* 120 (2016)  
28701–28711.



Cross-section tomograph

# Hybrid Approach

## Continuum Formulation

Water vapor

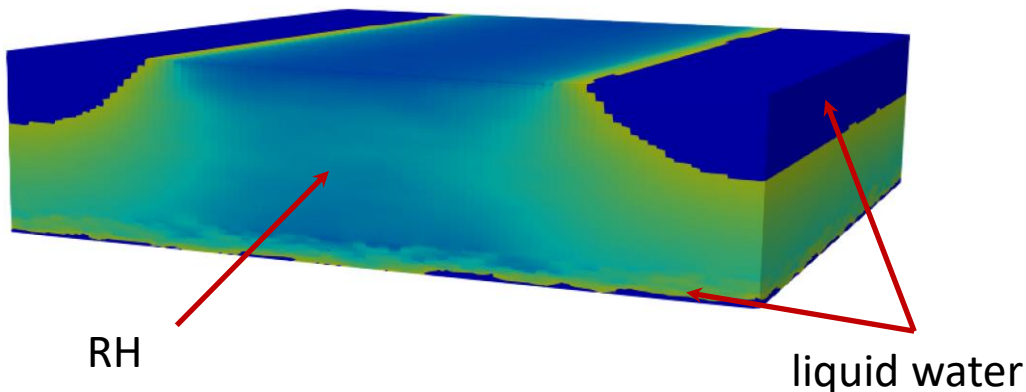
$$\nabla \cdot (-\bar{\bar{D}}_{wv,l}^{eff} \nabla C_{wv}) = S_{vl}$$

Temperature

$$\nabla \cdot (-\bar{k}_l^{eff}(s_l) \nabla T) = S_T$$

## Discrete Formulation

Liquid water (QSS Pore Network)

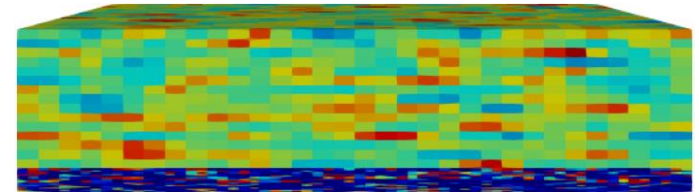


$$k_l^{eff} = k_l^{eff,dry} + (k_w - k_l^{eff,dry}) s_l$$

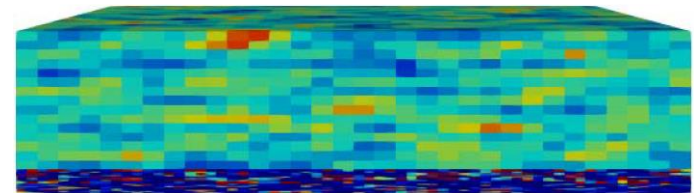
$$k_{l,gdl}^{eff,dry} = \begin{cases} 0.25 \text{ W m}^{-1}\text{K}^{-1} \text{ TP} \\ 5 \text{ W m}^{-1}\text{K}^{-1} \text{ IP} \end{cases}$$

$$k_{l,mpl/CL}^{eff,dry} = 0.1/0.22 \text{ W m}^{-1}\text{K}^{-1}$$

$$D_{wv,l}^{eff} \text{ (IP)}$$



$$D_{wv,l}^{eff} \text{ (TP)}$$

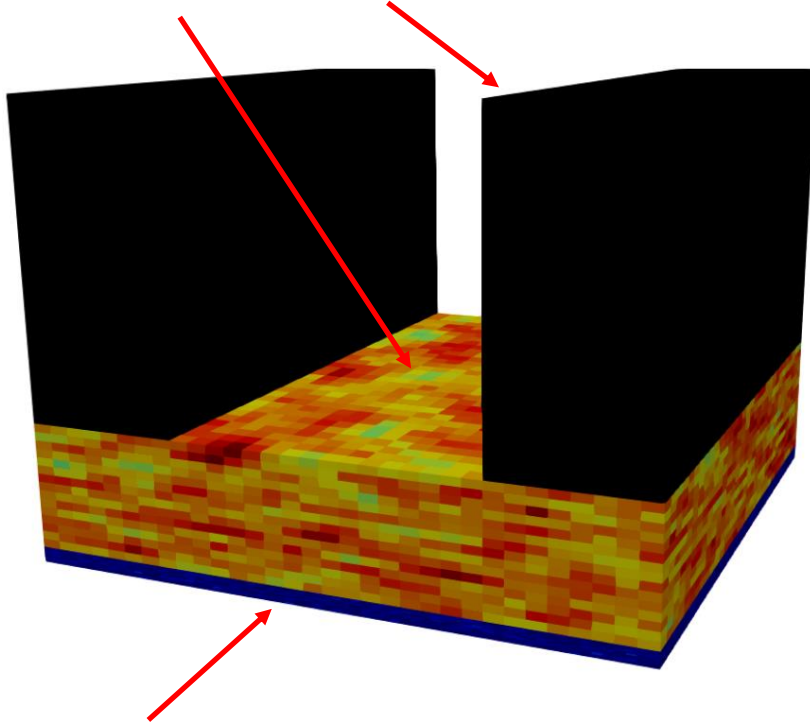


**Heterogeneous Knudsen  
diffusion induces water  
nucleation in CL**



# Boundary Conditions

$$C_{wv} = C_{wv}^{in}, T = T^{in} \text{ (imposed RH \& T)}$$



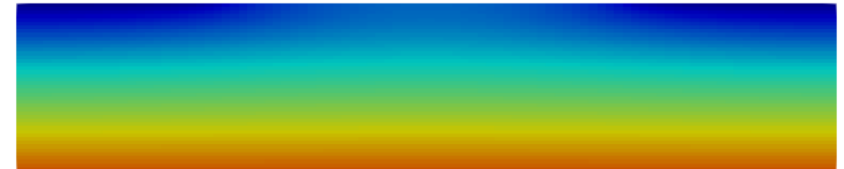
$$-\bar{\bar{D}}_{wv,l}^{eff} \nabla C_{wv} \cdot \mathbf{n} = -\beta \frac{I}{2F} \text{ (imposed water vapor flux)}$$

$$-\bar{\bar{k}}_l^{eff} \nabla T \cdot \mathbf{n} = -\left(\frac{h_{lv}}{2F} - V_{cell}\right) \frac{I}{2} \text{ (imposed heat flux)}$$

*RH*



*T*



**Water vapor and heat fluxes through CL are proportional to generated current density**

# Algorithm Evolution (Continuum/Discrete Coupling)

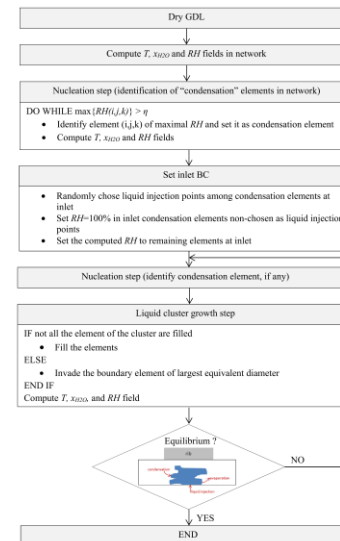
1. Determine **steady-state solution** for **continuum variables**.
2. Label **water clusters** and determine  $S_{vl,k} = \sum S_{vl}$  in each active water cluster.
3. If  $S_{vl,k} > 0$ , **invade** next CV with **minimum capillary resistance** in cluster  $k$ .  
If  $S_{vl,k} < 0$ , **remove** CV with **minimum capillary resistance** in cluster  $k$ .
4. Repeat Steps 1-3 until all water clusters either **reach the channel or show negligible mass change**,  $|S_{vl,k}| \leq \text{tol}$ ,  $\text{tol} = 10^{-16}$ .

## Main advantages

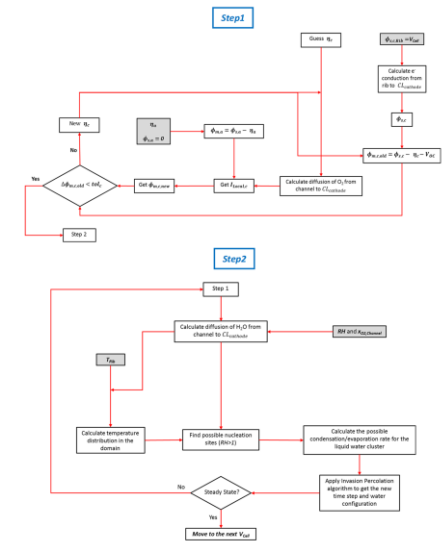
- Widespread availability of CFD software.
- Facilitated coupling of multiscale porous media assemblies.
- Simplified algorithm compared to previous fully PNM approaches.
- Step 1 can be easily adapted to describe transient gas transport evolution using a continuum CFD solver.



*Int. J. Heat Mass Trans.*  
47 (2019) 1043–1056.



*J. Appl. Electrochem.*  
47 (2017) 1323–1338.



# Source Terms

## Phase Change Mass Transfer

computed average saturation  
agrees with exp. data

If  $C_{wv} > C_{wv}^{sat}$  (condensation)  $\Rightarrow S_{vl} = k_{vl}(C_{wv} - C_{wv}^{sat}) > 0, \mathbf{s} = 1$

If  $C_{wv} \leq C_{wv}^{sat}$  (evaporation)  $\Rightarrow \begin{cases} s > 0 \text{ (wet): } S_{vl} = k_{vl}(C_{wv} - C_{wv}^{sat}) < 0, \mathbf{s} = 1 \\ s = 0 \text{ (dry): } S_{vl} = 0, \mathbf{s} = 0 \end{cases}$

## Phase Change Latent Heat

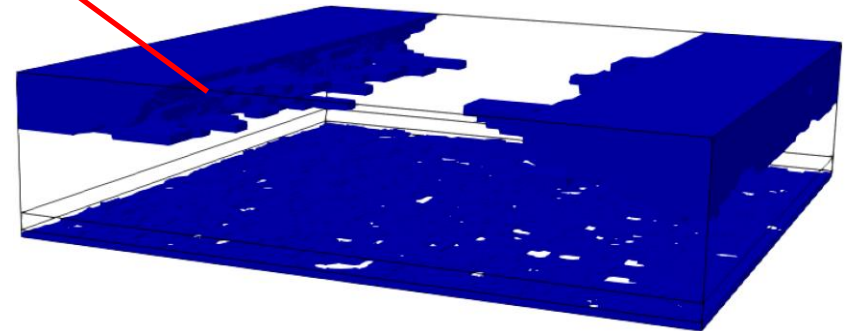
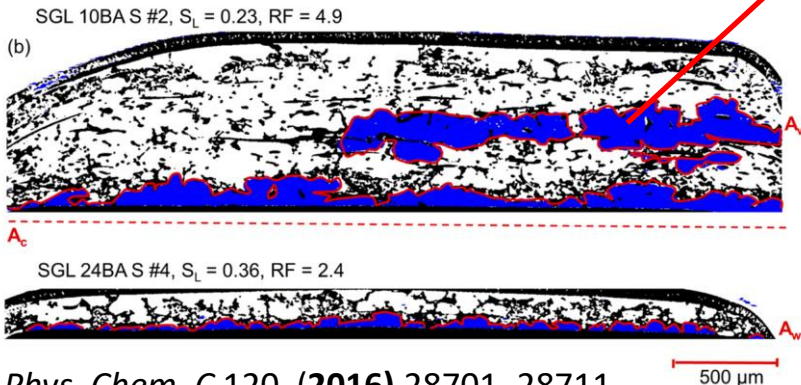
$$S_T = h_{vl}(T)S_{vl}, h_{vl}(T) = -2.44T + 3170.75 \text{ kJ kg}^{-1}$$

### Experimental

$RH \approx 1$  (local therm. eq.)

### Numerical

*weak spatial scale separation*



# Results I

$T = 80\text{ }^{\circ}\text{C}$ , High GDL Conductivity (e.g., Toray TGP-H-060)

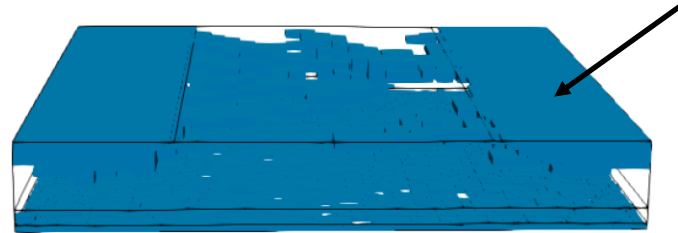
Experimental

A03  
 $0.75\text{ A/cm}^2$   
108% RH



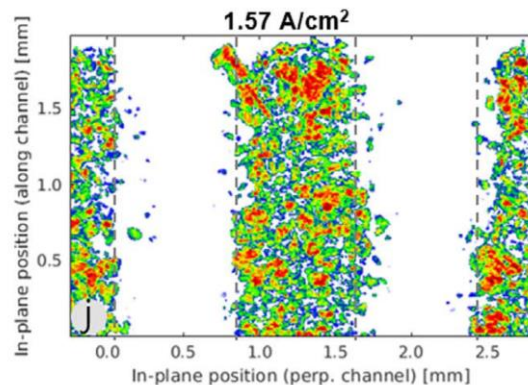
Numerical

mixed conditions



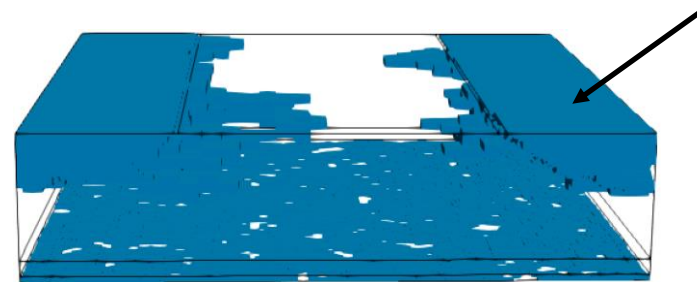
$T = 80\text{ }^{\circ}\text{C}$ , Low GDL Conductivity (e.g., Freudenberg)

Experimental



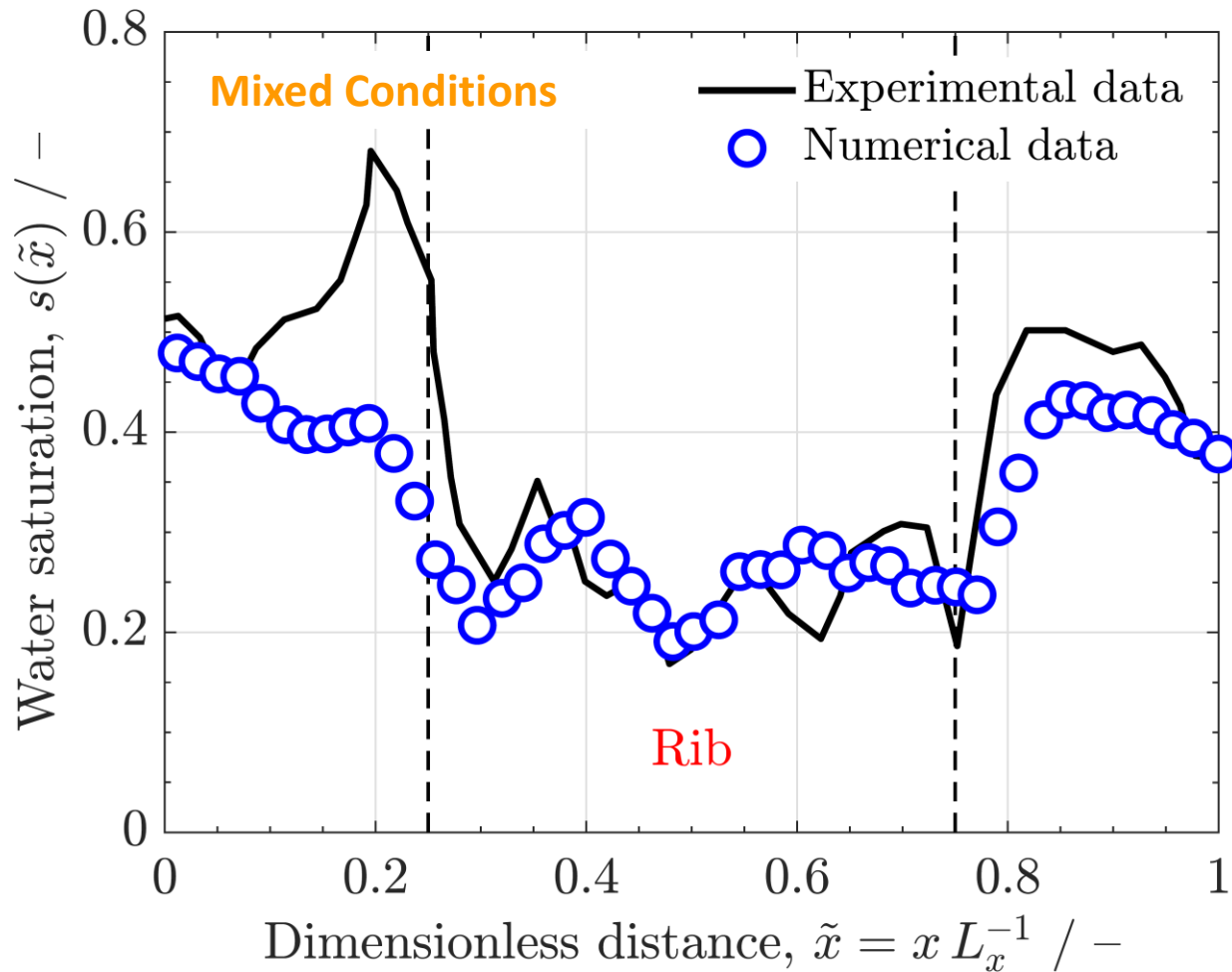
Numerical

preferential condensation under rib





## Results II

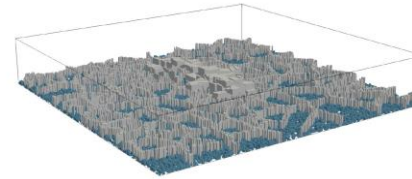
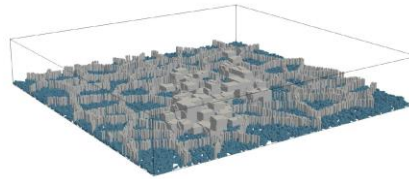
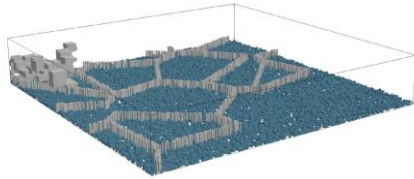


$I = 0.75 \text{ A cm}^{-2}$ ,  $\text{RH}^{in} = 0.99$ ,  $T^{in} = 80 \text{ }^\circ\text{C}$ , Toray TGP-H-060

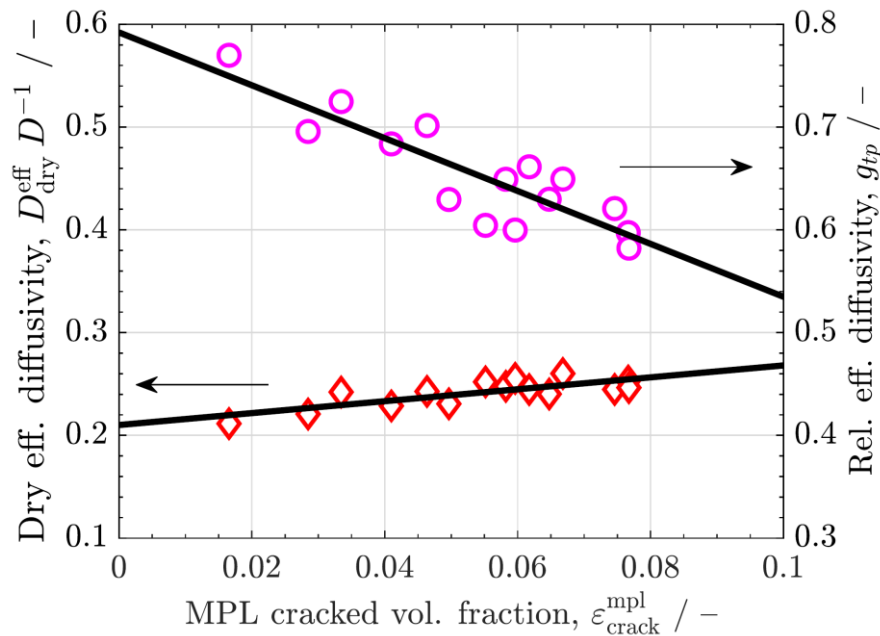
# First Insight on Cracks

- Two regimes: Mono- vs. Multi-crack Invasion

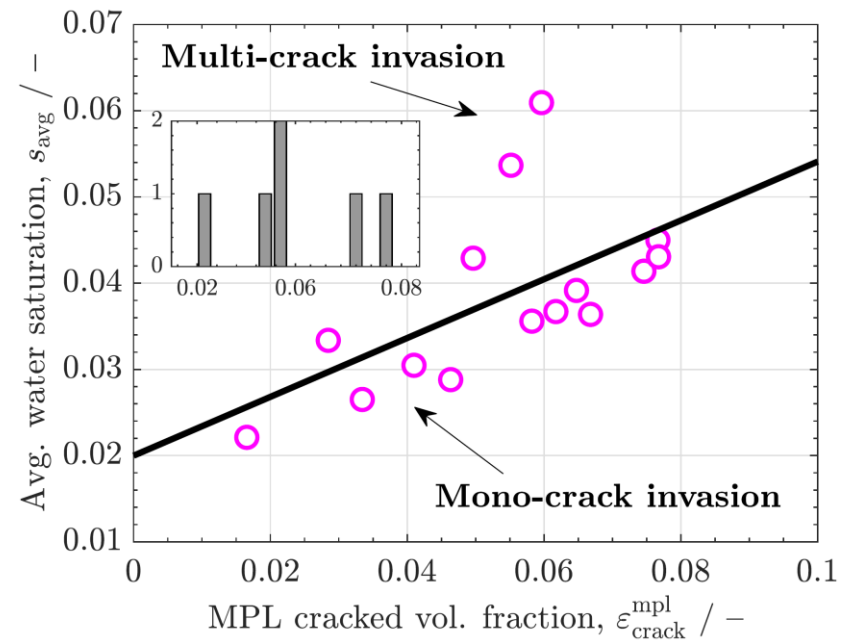
increasing crack density



## Diffusivity



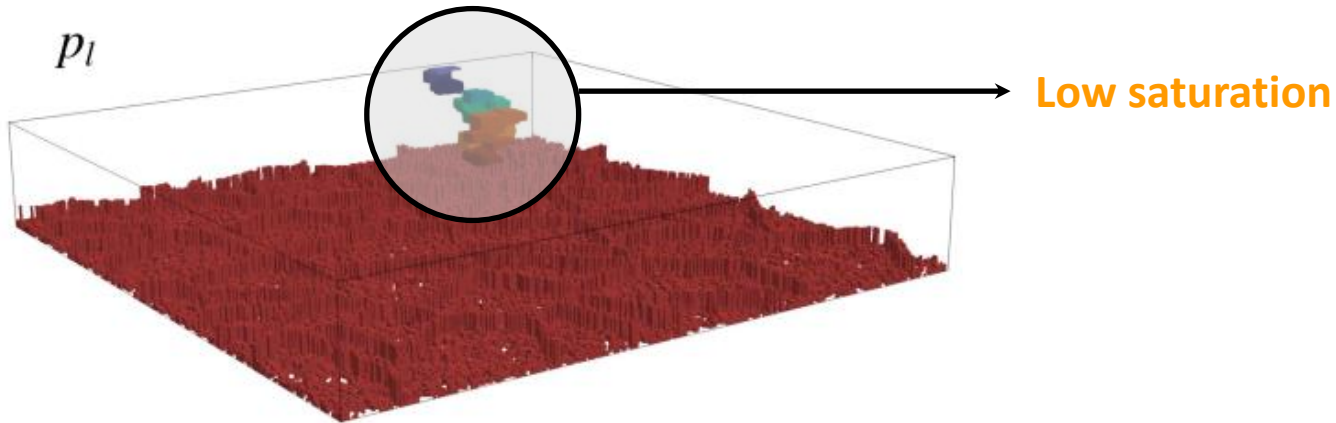
## Saturation



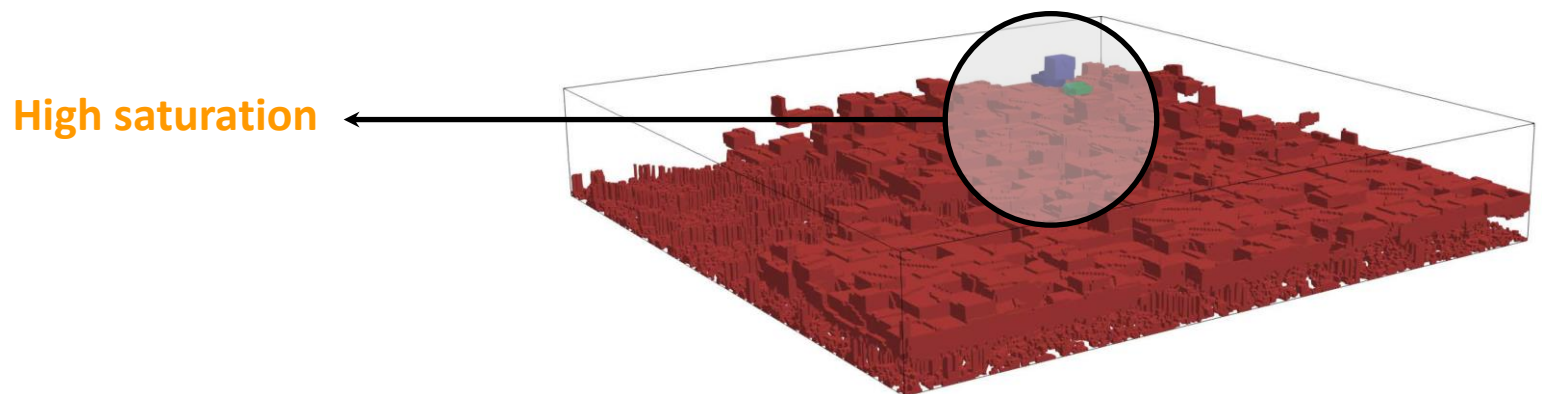
# First Insight on Cracks

- **Two regimes:** Mono- vs. Multi-crack Invasion

**Mono-crack invasion**

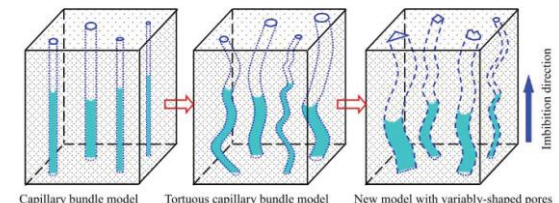
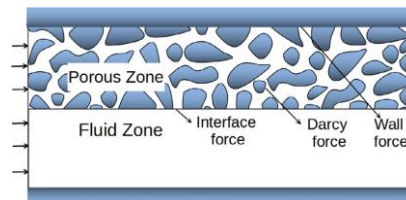
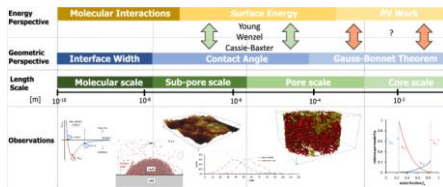


**Multi-crack invasion**



# Conclusions & Future Work

- A hybrid (continuum/discrete) formulation is a convenient framework to describe heterogeneous porous media without (GDL) and with (MPL & CL) separation between pore and layer scales.
- Significantly lower characteristic time of phase change kinetics compared to gas diffusion and capillary transport allows quasi-steady-state simplification.
- Development of unitized MEAs can dramatically enhance volume power density.
- Cracks show a bifunctional behavior (mono- vs. Multi-crack invasion).
- Incorporate electrochemistry (fully coupled model).
- Analyze effect of multi-layer wetting properties.
- Include interaction w/ flow field.
- Coupling w/ multi-scale bundle of capillary tubes for CL and MPL.





# Thank you very much for your attention!!!

