



Matrix-fracture flow transfer in fractured porous media: experiments and simulations

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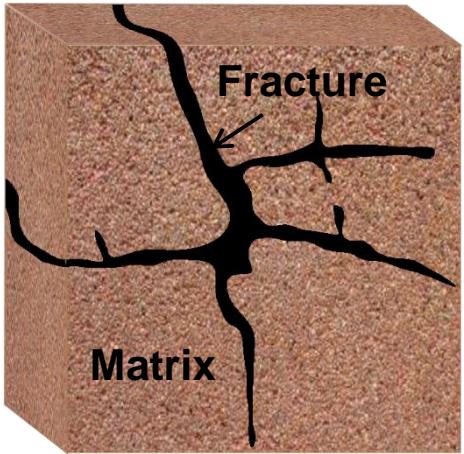
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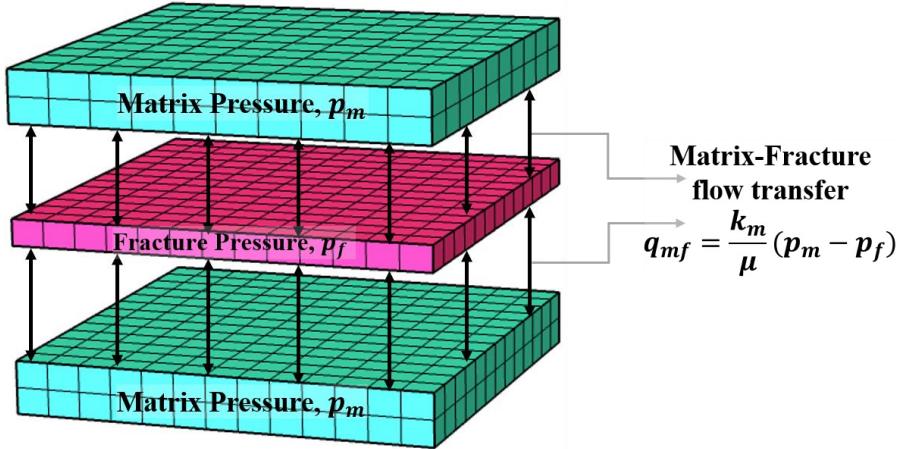
OUTLINE

1. Introduction
2. Experiments of matrix-fracture transfer
3. Generalized flow transfer model
4. Effect of influencing factors
5. Concluding remarks

1. Introduction



Matrix and fracture structure
in fractured porous media

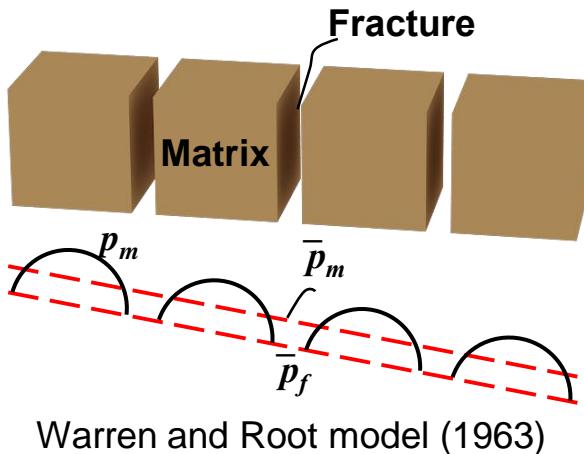


Matrix-fracture flow transfer

- The **matrix-fracture flow transfer** is one of the most important characteristics of flow in fractured porous media
- When the fluid pressure on matrix is different from that on the fracture, the fluid will transfer from matrix to fracture, or vice versa
- The phenomenon is usually described using a **transfer function**

1. Introduction

❖ Transfer function in dual-porosity model



Transfer function:

$$q_{mf} = \sigma \frac{k_m}{\mu} \left(\overline{p}_m - \overline{p}_f \right)$$

Where: p_m = average matrix pressure;

\overline{p}_f = average fracture pressure;

σ = shape factor ($1/L^2$).

Values of dimensionless shape factors σL^2

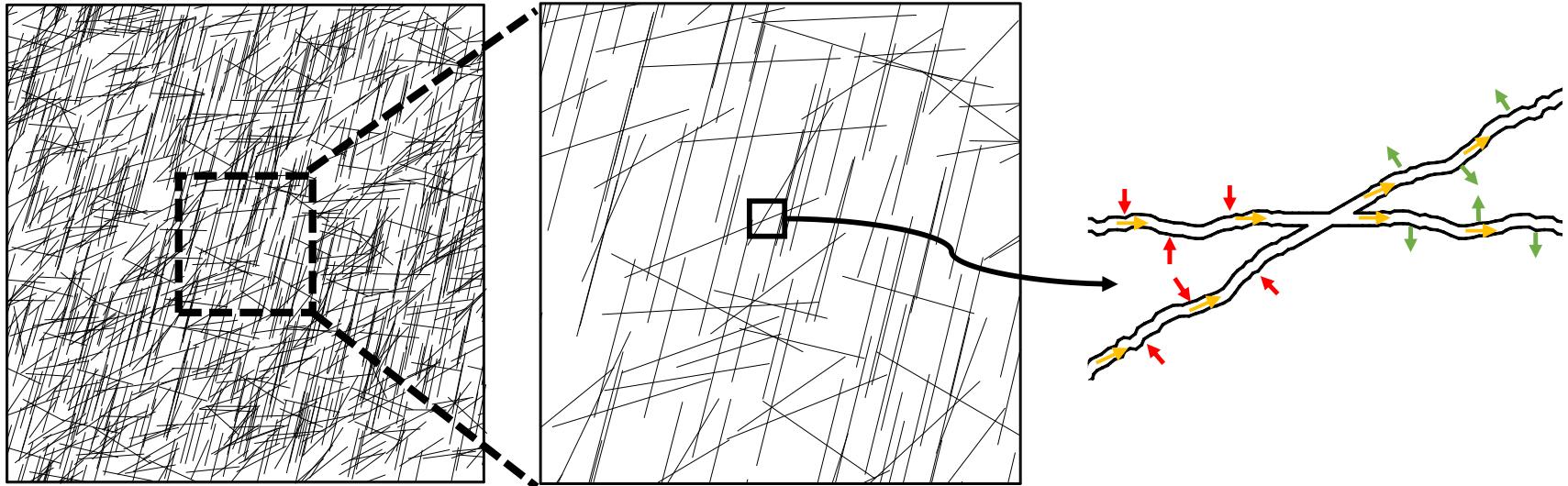
References	σL^2
Warren-Root (1963)	60
Kazemi et al. (1976)	12
Coats (1989)	49.58
Zimmerman et al. (1993)	29.61
Lim and Aziz (1995)	29.61
Sarda et al.(2001)	48
Hassanzadeh and Pooladi-Darvish (2006)	25.56
Mora and Wattenbarger (2009)	25.67
Hassanzadeh et al. (2009)	25.67
Peyman et al. (2020)	15.6

Note: L =characteristic length of the matrix

- ◆ It is ambiguous for engineers to apply these findings in practice
- ◆ It's need to propose a generalized Matrix-fracture transfer function with consistent parameters

1. Introduction

❖ Content of the study

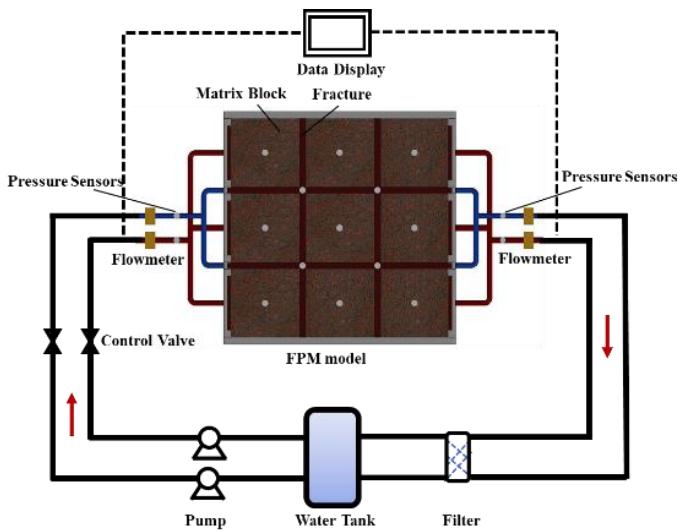
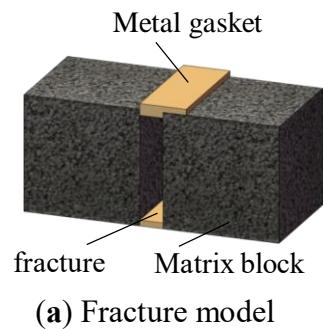
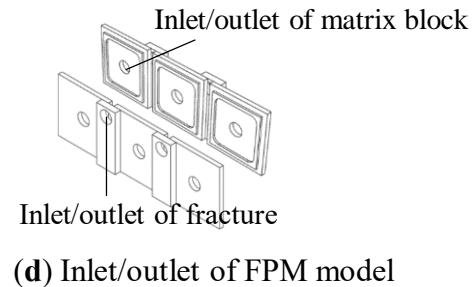
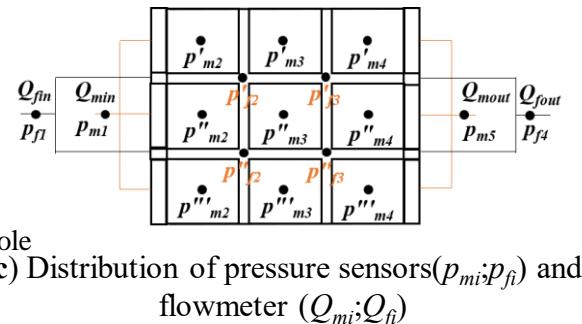
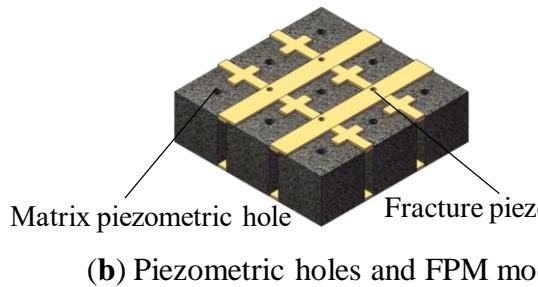


Variable flow transfer direction in fractured porous media with complex geometry

- Study of matrix-fracture flow transfer by experiment and simulation
- Matrix-fracture flow transfer model
- Investigate the influence of the fracture occurrence and fracture-matrix permeability ratio on matrix-fracture flow transfer

2. Experiments of matrix-fracture transfer

❖ Test equipment



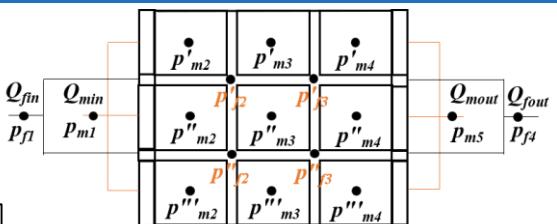
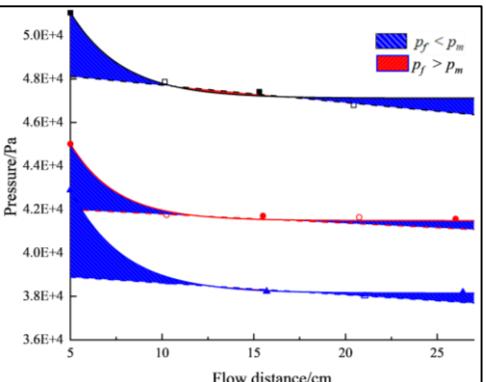
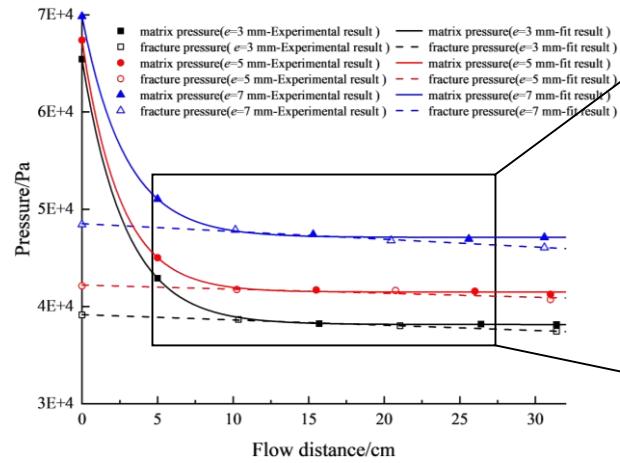
Schematic diagram for matrix-fracture flow transfer in FPM

- FPM model consists of 9 cubic matrix blocks and 4 mutually orthogonal fractures
- Parameters: $e = 3 \text{ mm}$; $e = 5 \text{ mm}$; $e = 7 \text{ mm}$ ($V_m = 100 \times 100 \times 100 \text{ mm}^3$; $k_m = 1.47 \times 10^{-4} \text{ m/s}$)

2. Experiments of matrix-fracture transfer

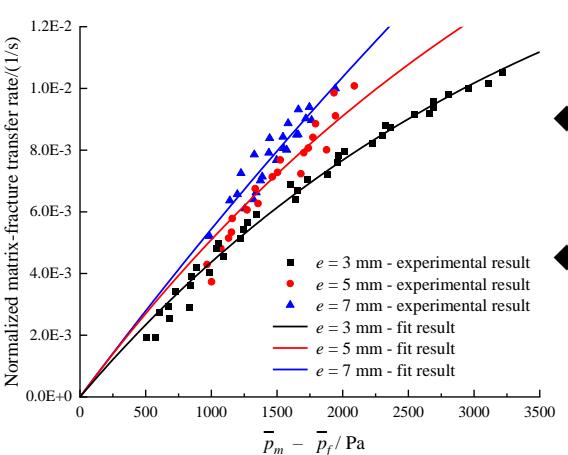
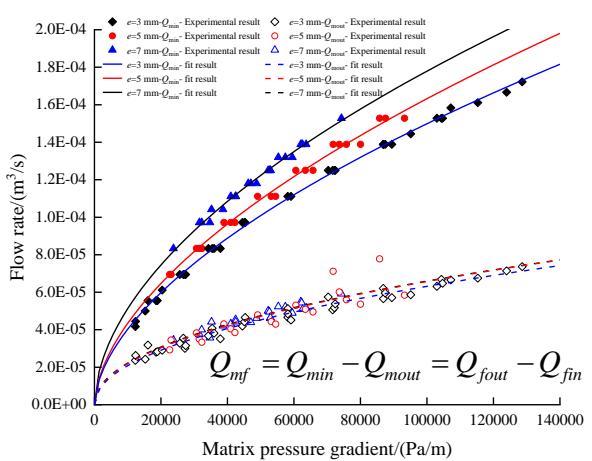
❖ Experimental results and discussion

- Pressure distribution of matrix and fracture



- ◆ More than 90% of the pressure drop is concentrated in the first half of the flow distance
- ◆ Matrix-fracture flow transfer mainly occurs in the first half of the flow distance

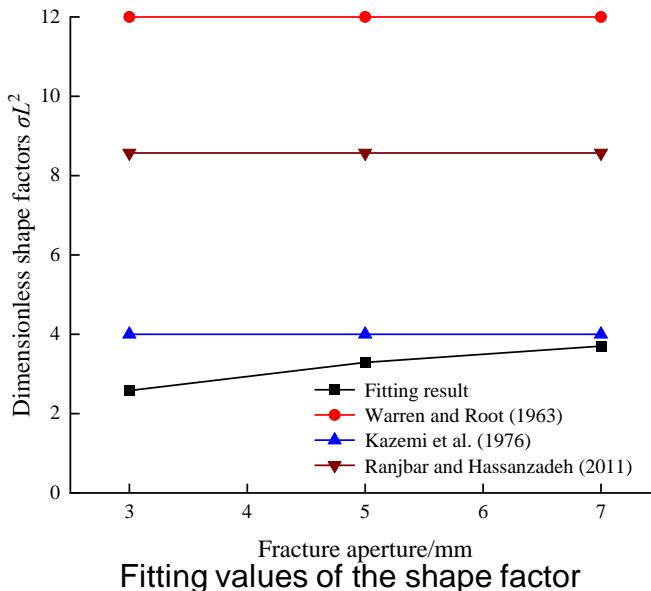
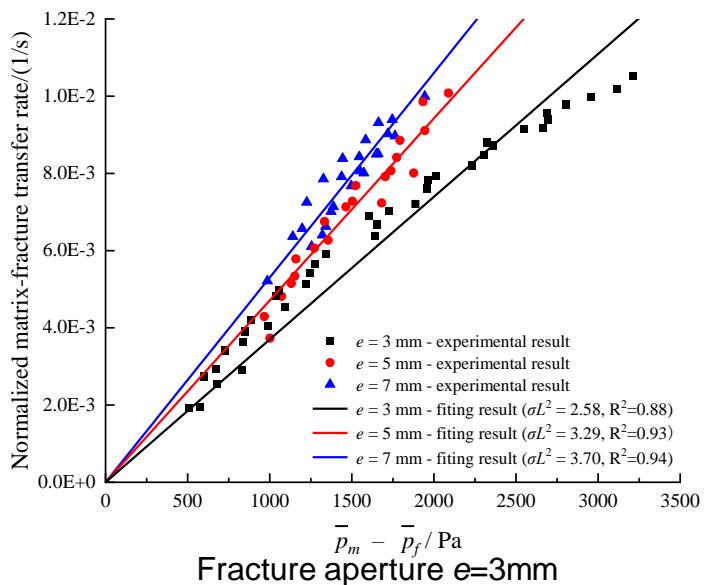
➤ Distribution of outlet flow rate



- ◆ The matrix-fracture flow transfer rate accounts for 43%~63% of the matrix inlet flow rate
- ◆ The normalized matrix-fracture flow transfer rate increases with fracture aperture, matrix-fracture pressure difference

2. Experiments of matrix-fracture transfer

- ❖ Matrix-fracture transfer rate
 - Transfer function with shape factor



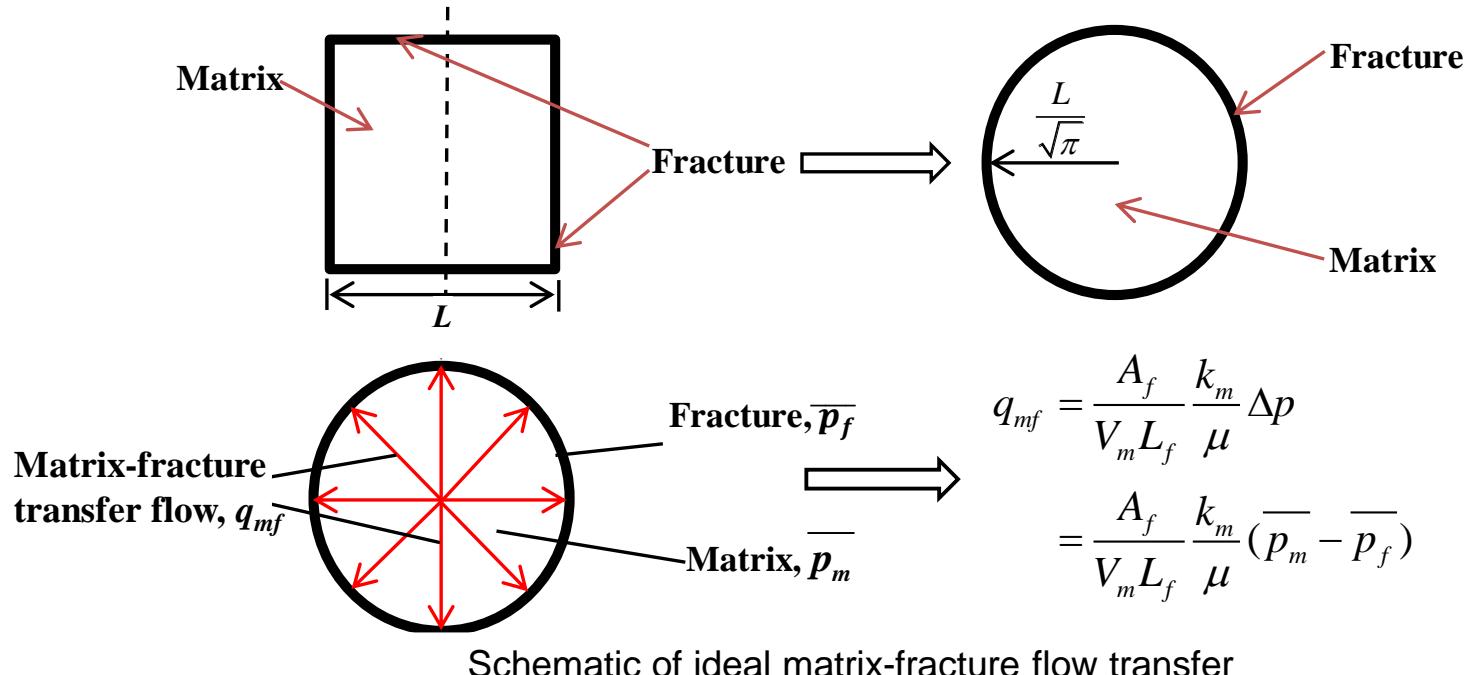
Transfer function: $q_{mf} = \sigma \frac{k_m}{\mu} \left(\bar{p}_m - \bar{p}_f \right)$

- ◆ The shape factor increases with increasing fracture aperture (2.58~3.70).
- ◆ The prediction of the Kazemi model is better than that of Warren-Root model.
- ◆ The predictions gradually becomes worse as $\bar{p}_m - \bar{p}_f$ increases

3. Generalized flow transfer model

- ❖ A generalized matrix-fracture flow transfer model

- Ideal matrix-fracture flow transfer



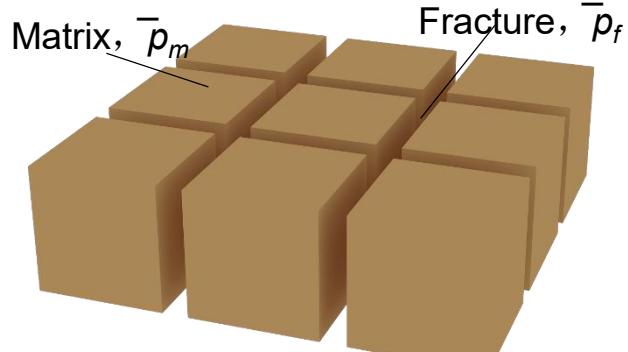
Assumptions:

- ◆ Transfer flow occurs at the matrix/fracture interface
- ◆ Flow transfer is at steady state
- ◆ The matrix-fracture transfer flow is governed by Darcy's law
- ◆ The flow in the entire block are assumed to be one-way

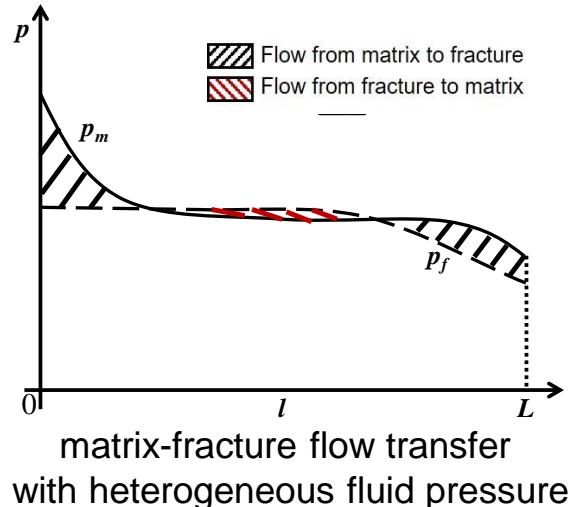
3. Generalized flow transfer model

- ❖ A generalized matrix-fracture flow transfer model

- Matrix-fracture flow transfer with regularly distributed fractures



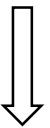
Fractured porous media



Ideal flow transfer:

$$q_{mf} = \frac{A_f}{V_m L_f} \frac{k_m}{\mu} (\bar{p}_m - \bar{p}_f)$$

heterogeneous fluid pressure



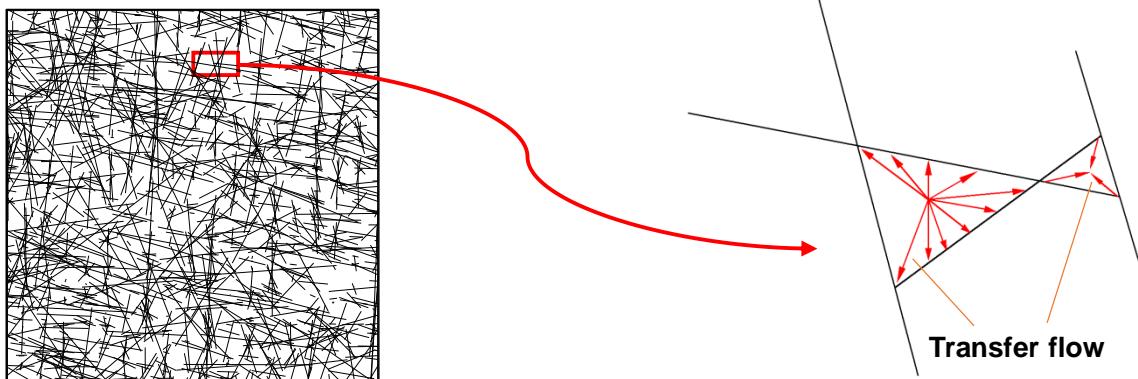
fracture pressure correction coefficient α

$$q_{mf} = \frac{A_f}{V_m L_f} \frac{k_m}{\mu} (\bar{p}_m - \alpha \bar{p}_f)$$

Where: $\bar{p}_m - \alpha \bar{p}_f$ = effective pressure difference between matrix and fracture;

3. Generalized flow transfer model

- ❖ A generalized matrix-fracture flow transfer model
 - Matrix-fracture flow transfer with irregularly distributed fractures



Schematic of matrix-fracture flow transfer with irregularly distributed fractures

$$\text{Ideal transfer flow: } q_{mf} = \frac{A_f}{V_m L_f} \frac{k_m}{\mu} (\bar{p}_m - \bar{p}_f) \xrightarrow{\text{heterogeneous pressure}} q_{mf} = \frac{A_f}{V_m L_f} \frac{k_m}{\mu} (\bar{p}_m - \alpha \bar{p}_f)$$

Natural rock

$$\frac{A_f}{V_m L_f} \rightarrow \frac{1}{l_c^2}$$

Generalized flow transfer model:

$$q_{mf} = \frac{1}{l_c^2} \frac{k_m}{\mu} (\bar{p}_m - \alpha \bar{p}_f)$$

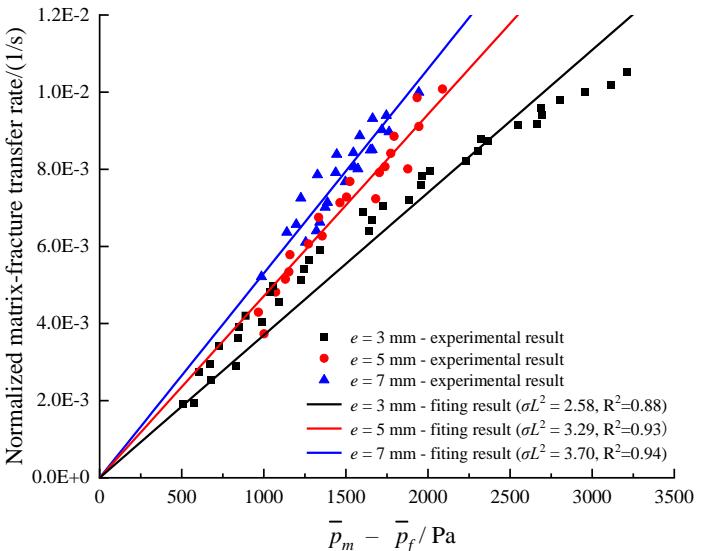
Where: l_c = Characteristic trace length of fractures;

$\bar{p}_m - \alpha \bar{p}_f$ = Effective pressure difference between matrix and fracture;

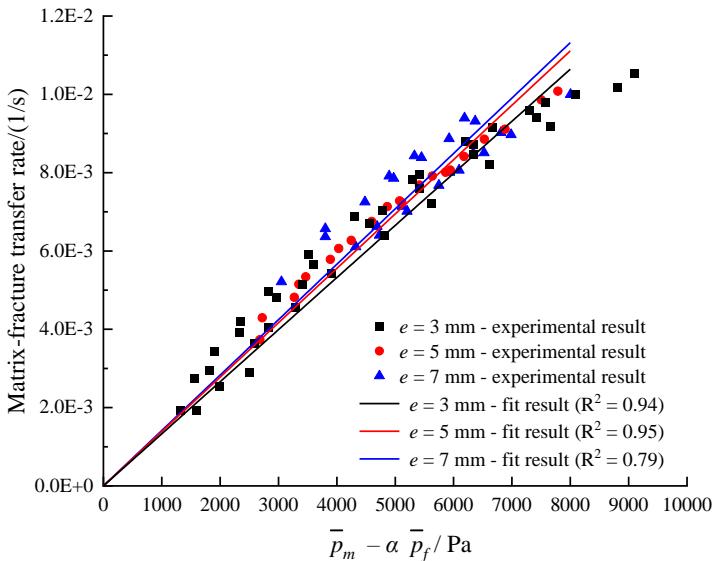
3. Generalized flow transfer model

- ❖ Verification of generalized matrix-fracture flow transfer model
 - Generalized matrix-fracture flow transfer model

$$q_{mf} = \frac{1}{l_c^2} \frac{k_m}{\mu} \left(\bar{p}_m - \alpha \bar{p}_f \right)$$



Shape factor model



Generalized transfer model

- ◆ The flow transfer rate has a linear relationship with the effective matrix-fracture pressure difference, but it cannot reflect the influence of the fracture aperture

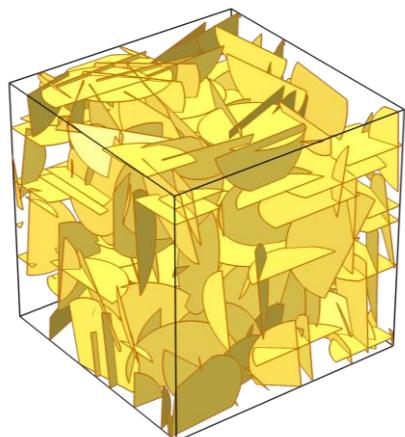
4. Effect of influencing factors

❖ Simulation method

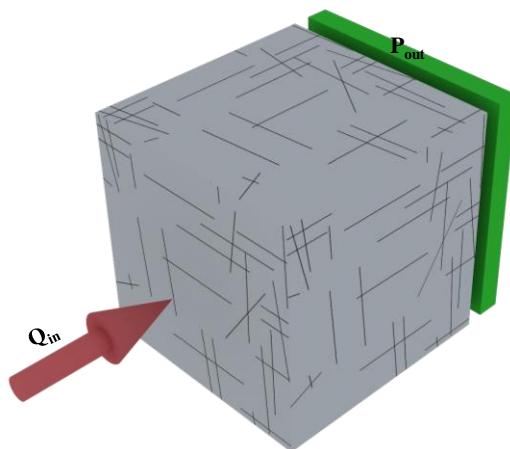
- The parameter values of fracture network (Hitchmough et al., 2007)

parameter	Trace length/m	Dip angle/ $^{\circ}$	Dip direction/ $^{\circ}$	Density/(pieces/m $^{-3}$)	aperture/mm
Mean	4	3, 89, 85	90, 265, 351	0.1	0.2
Variance	0.1	1, 8, 10	5, 29, 14	—	—
Distribution	Normal	Normal	Normal	—	—

- Geometrical model and boundary conditions



Geometrical model
(10×10×10 m)



Boundary conditions

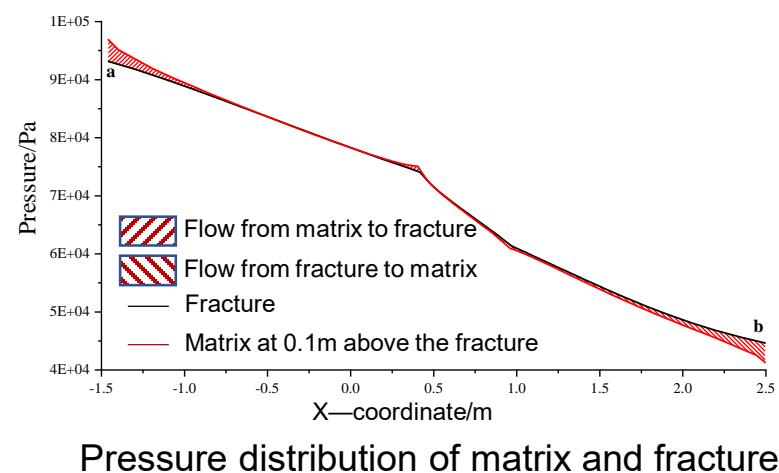
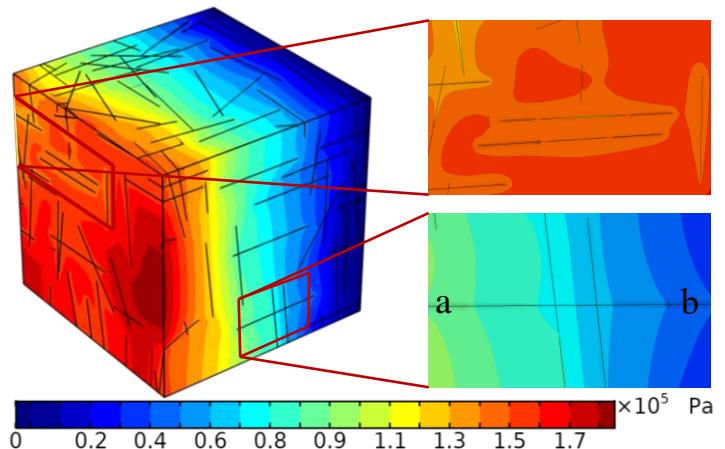
- Simulation cases performed in this study

NO.	Trace length/m	Density/(pieces/m $^{-3}$)	K_t/k_m
1	4	0.1	10000
2	3.5	0.1	10000
3	4.5	0.1	10000
4	4	0.05	10000
5	4	0.15	10000
6	4	0.1	5000
7	4	0.1	20000

4. Effect of influencing factors

❖ Simulation results and discussion

➤ Distribution of matrix and fracture



The heterogeneous fluid pressure due to the difference of permeability between matrix and fracture:

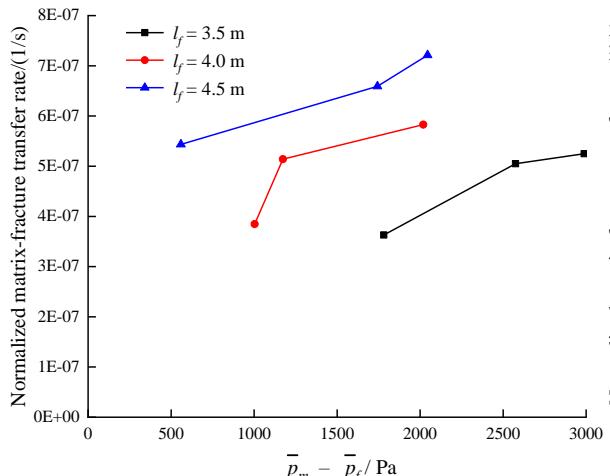
- ◆ **High pressure**: area away the fracture
- ◆ **Medium pressure**: the matrix area near the fracture
- ◆ **Low pressure**: area near the fracture

- ◆ Peaks and troughs appear in the matrix pressure curve along the flow direction due to the complexity of fracture geometry
- ◆ **Inconsistent directions** of matrix-fracture flow transfer because of the **heterogeneous fluid pressure** around the matrix

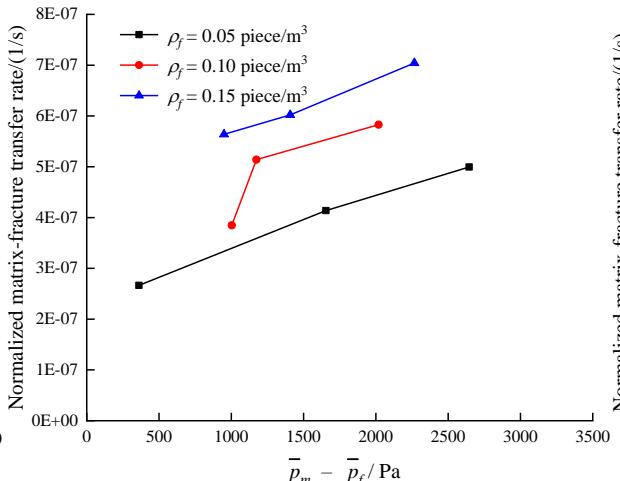
4. Effect of influencing factors

❖ Discussion of simulation results

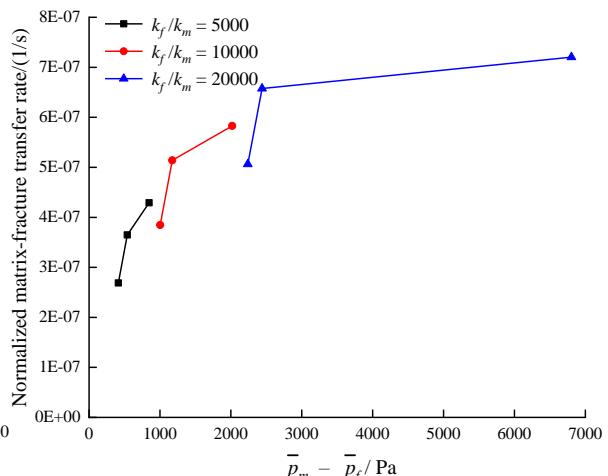
➤ Effect of influencing factors



Relations between matrix-fracture pressure difference and matrix-fracture flow transfer with different fracture trace lengths



Relations between matrix-fracture pressure difference and matrix-fracture flow transfer with different fracture density



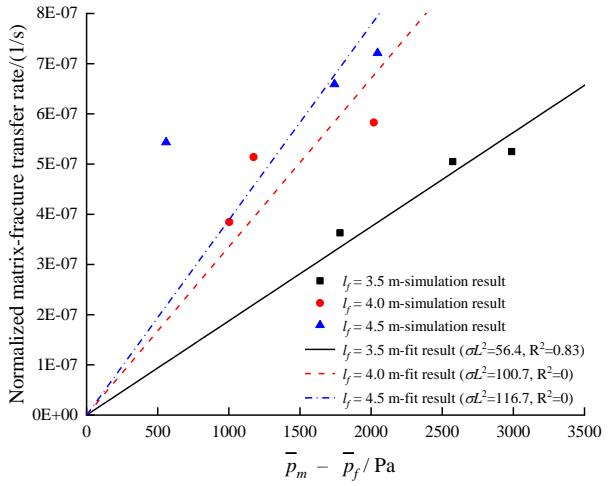
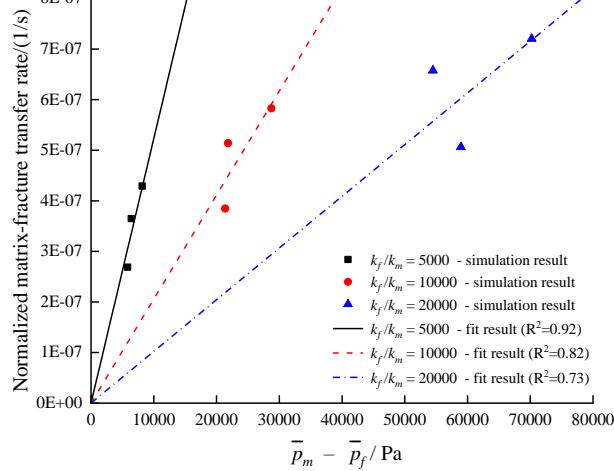
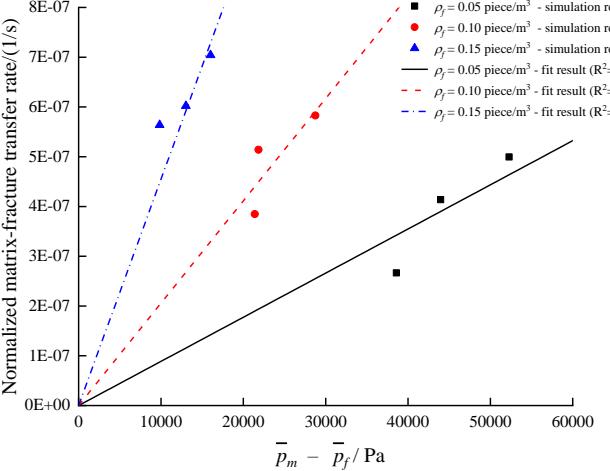
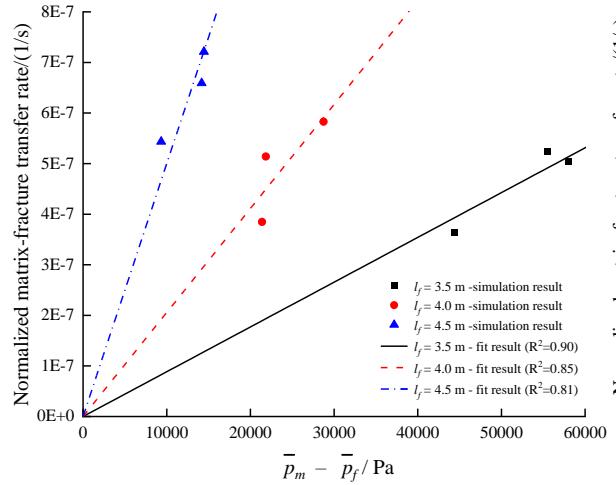
Relations between matrix-fracture pressure difference and matrix-fracture flow transfer with different fracture/matrix permeability ratio

- ◆ The flow transfer rate presented a **nonlinear increasing trend** as the matrix-fracture pressure difference increased.
- ◆ The fracture aperture, trace length, and density have a **positive effect** on the flow transfer, and the FMPR has a **negative effect** on the flow transfer.

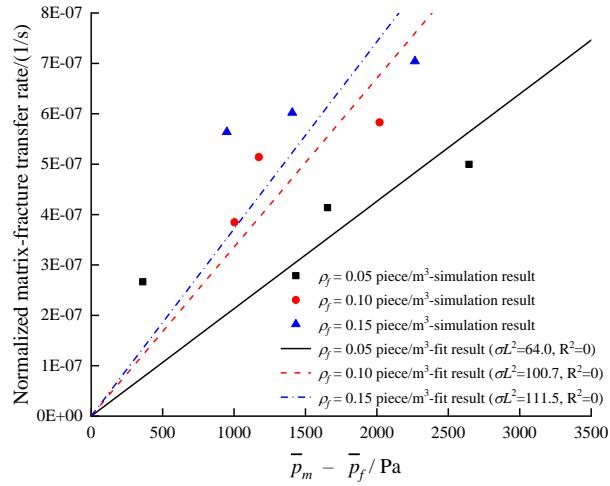
4. Effect of influencing factors

❖ Discussion of simulation results

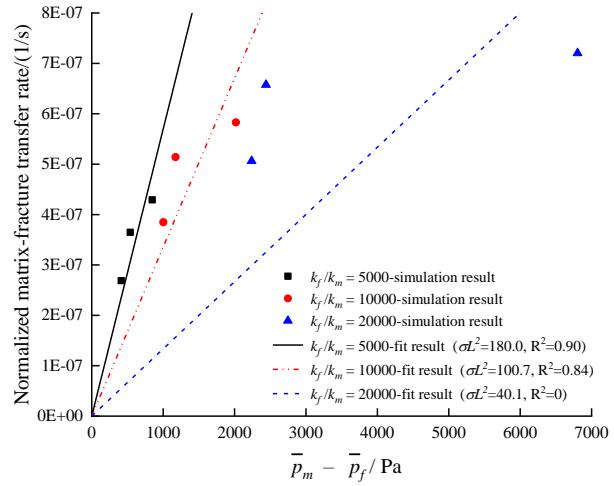
➤ Verification of the flow transfer model



Influence of fracture trace length



Influence of fracture density



Influence of fracture/matrix permeability ratio



5. Concluding remarks

- Experiments of matrix-fracture flow transfer in fractured porous media were performed under different aperture and pressure difference between matrix and fracture. The experiments show that there is a strong nonlinear relationship between the matrix-fracture flow transfer term and flow rates.
- A generalized matrix-fracture flow transfer model for fractured porous media considering the influence of the stochastic fracture distribution on fluid flow was proposed. The matrix-fracture flow transfer term depends on the effective pressure difference between matrix and fracture.
- The influence of fracture trace length, density, and fracture/matrix permeability ratio on the matrix-fracture flow transfer term were investigated by simulation. The matrix-fracture flow transfer term increases with the increase of fracture trace length, density, and fracture/matrix permeability ratio, while the fracture pressure correction coefficient is opposite.



— Thank you! —

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