



Don't miss a moment!

Simple models of soil hydraulic properties in the complete moisture range: Testing the new PDI model system with a comprehensive experimental dataset

Wolfgang Durner, Tobias L. Hohenbrink, Sascha C. Iden, Andre Peters



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Where I first met Harry



Bayreuth Festspielhaus



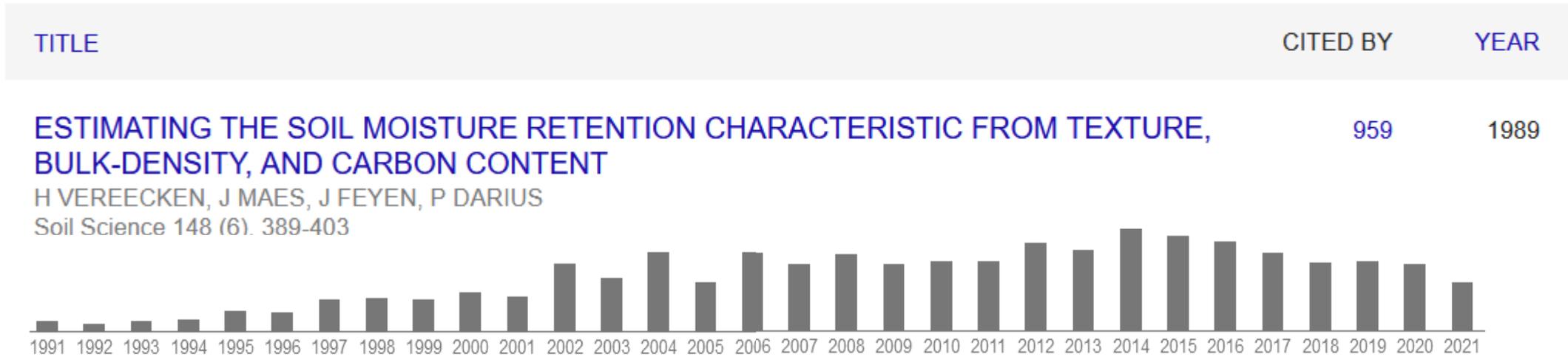
Pedotransferfunctions, PTF



Vereecken Harry

Professor [Forschungszentrum Juelich](#)
Verified email at fz-juelich.de - [Homepage](#)
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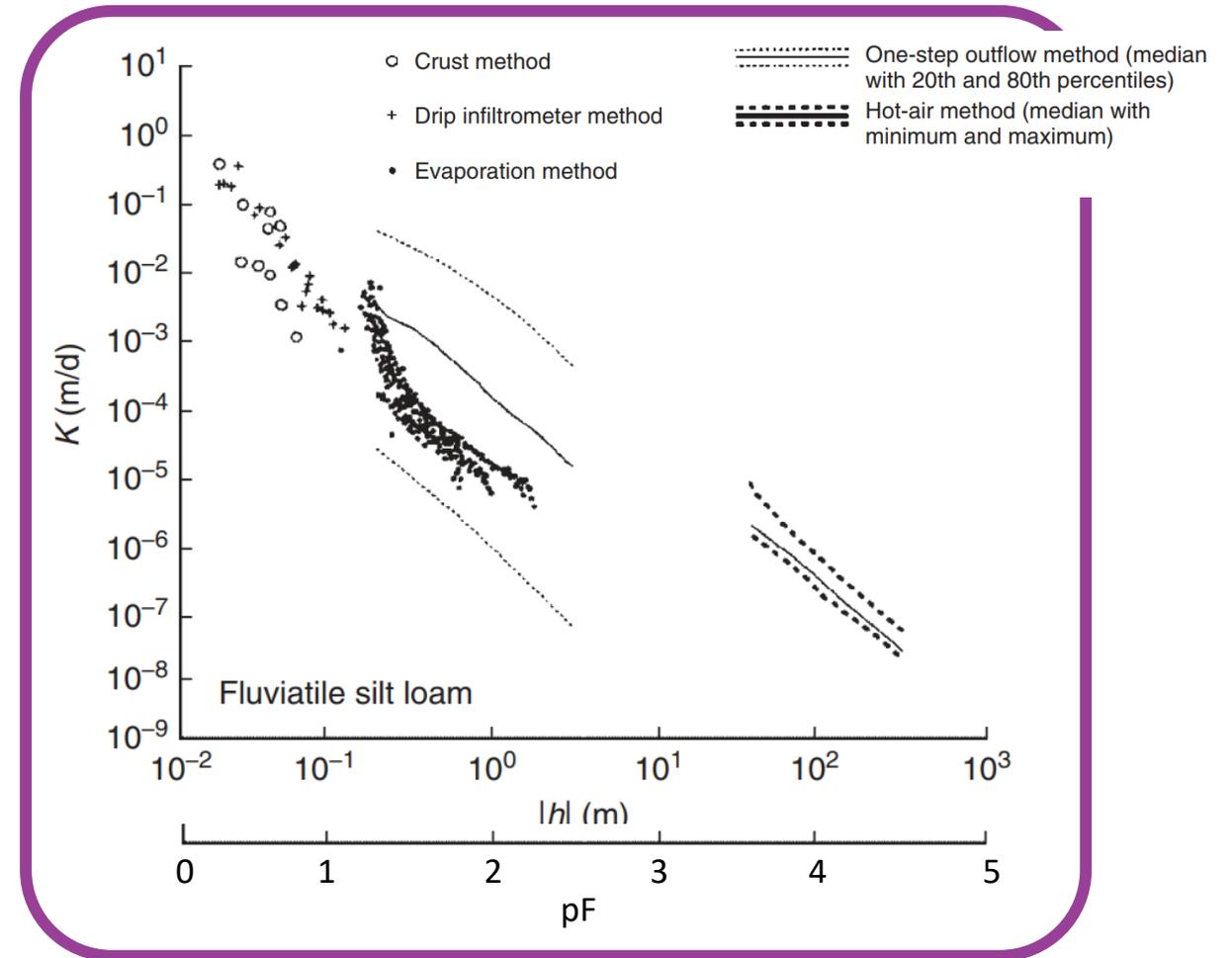
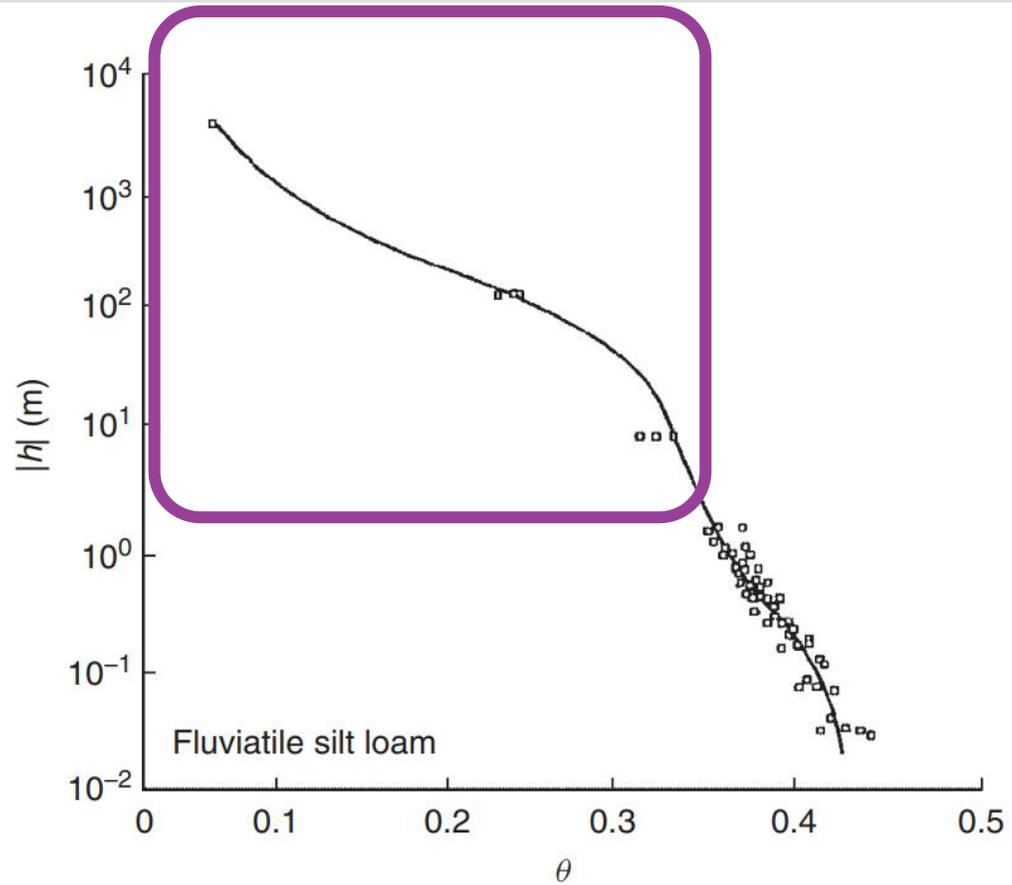
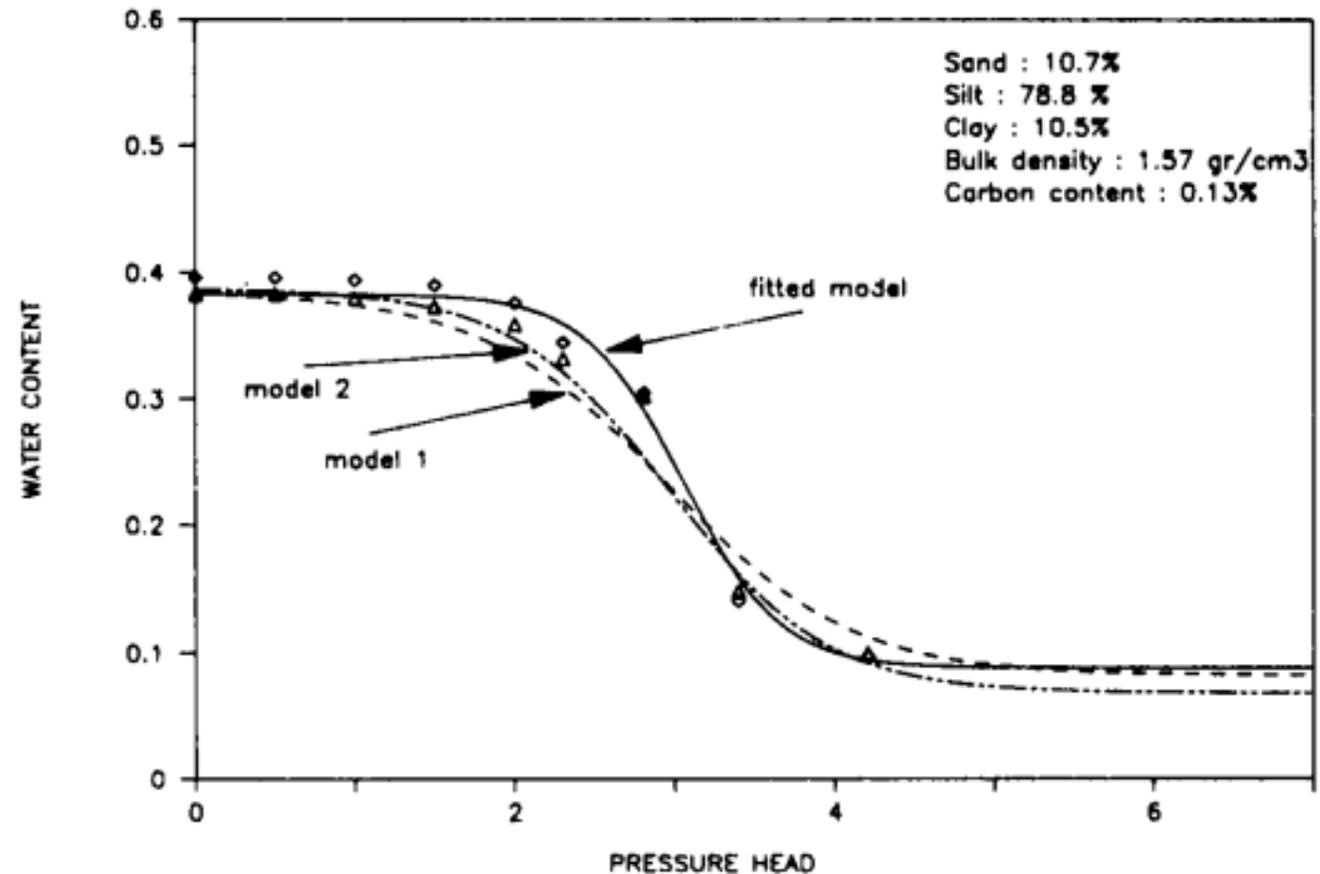


Figure 1 Hydraulic properties of a fluvatile silt loam. (a) Water retention curve measurements. (b) Unsaturated conductivity measurements, determined by five different methods (Reproduced from Stolte *et al.*, 1994 by permission of Soil Science Society of America)



FIG. 4. Estimated moisture retention characteristics with two sets of regression equations (models 1 and 2) and fitted moisture retention characteristic for a sandy soil. The parameter vector of the fitted model equals: $\theta_r = 0.020$; $\theta_s = 0.325$; $\alpha = 0.0185$; $n = 2.993$. The data points are indicated by squares and triangles.

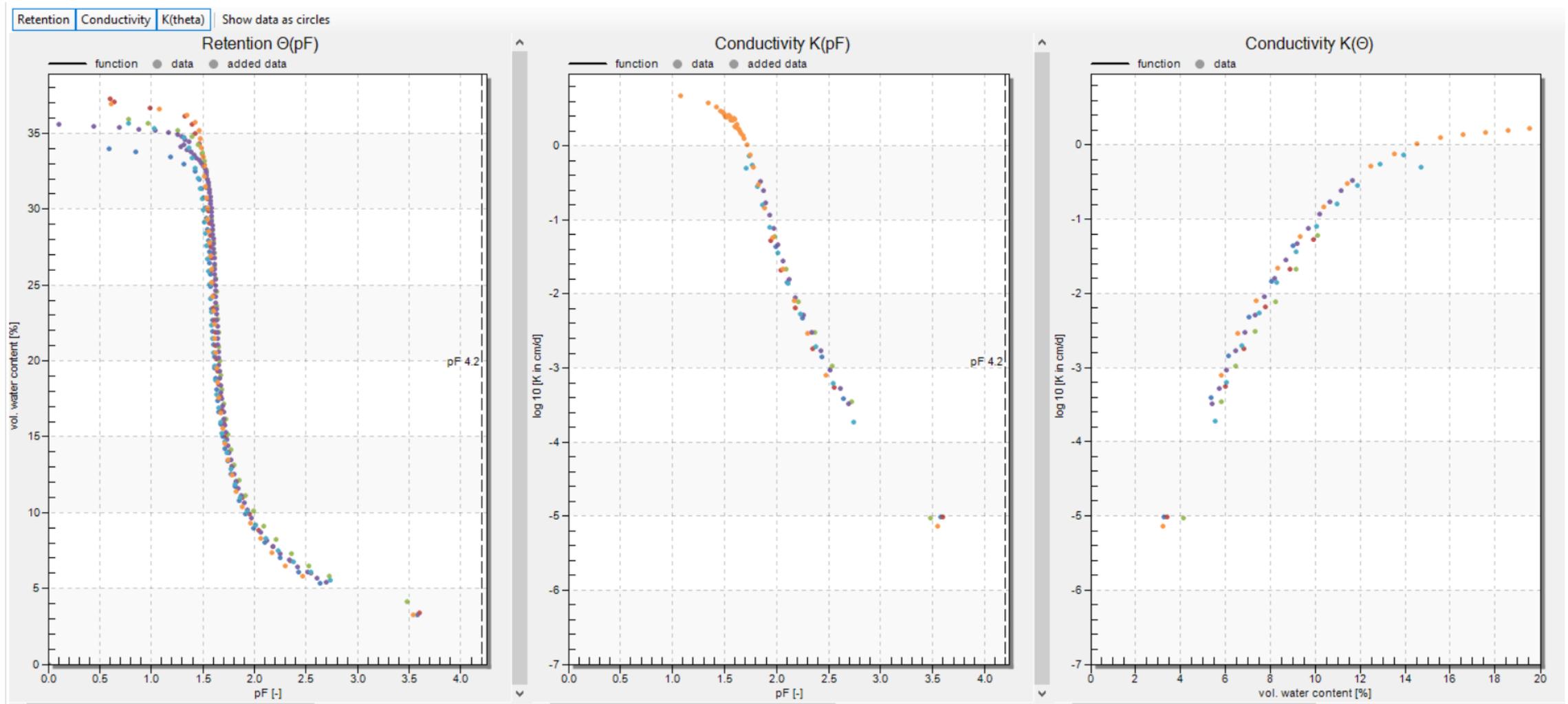


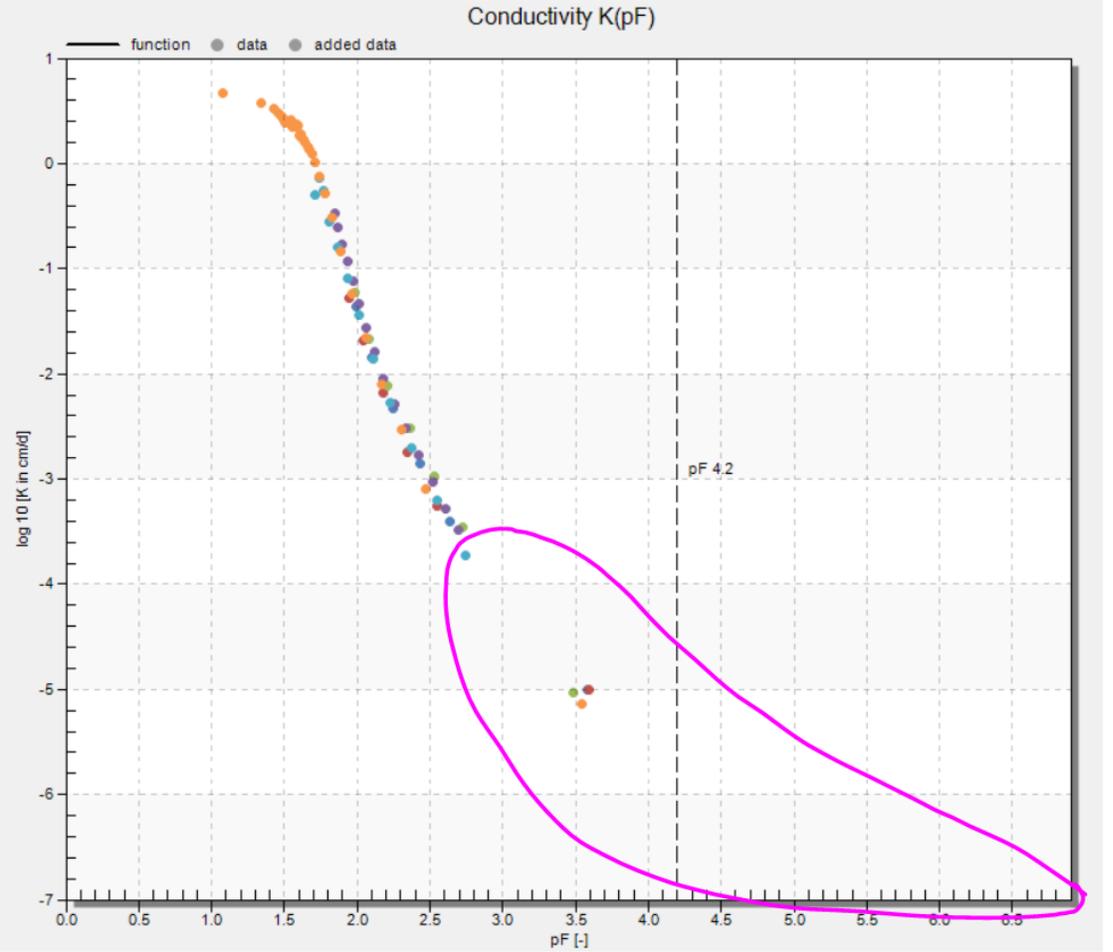
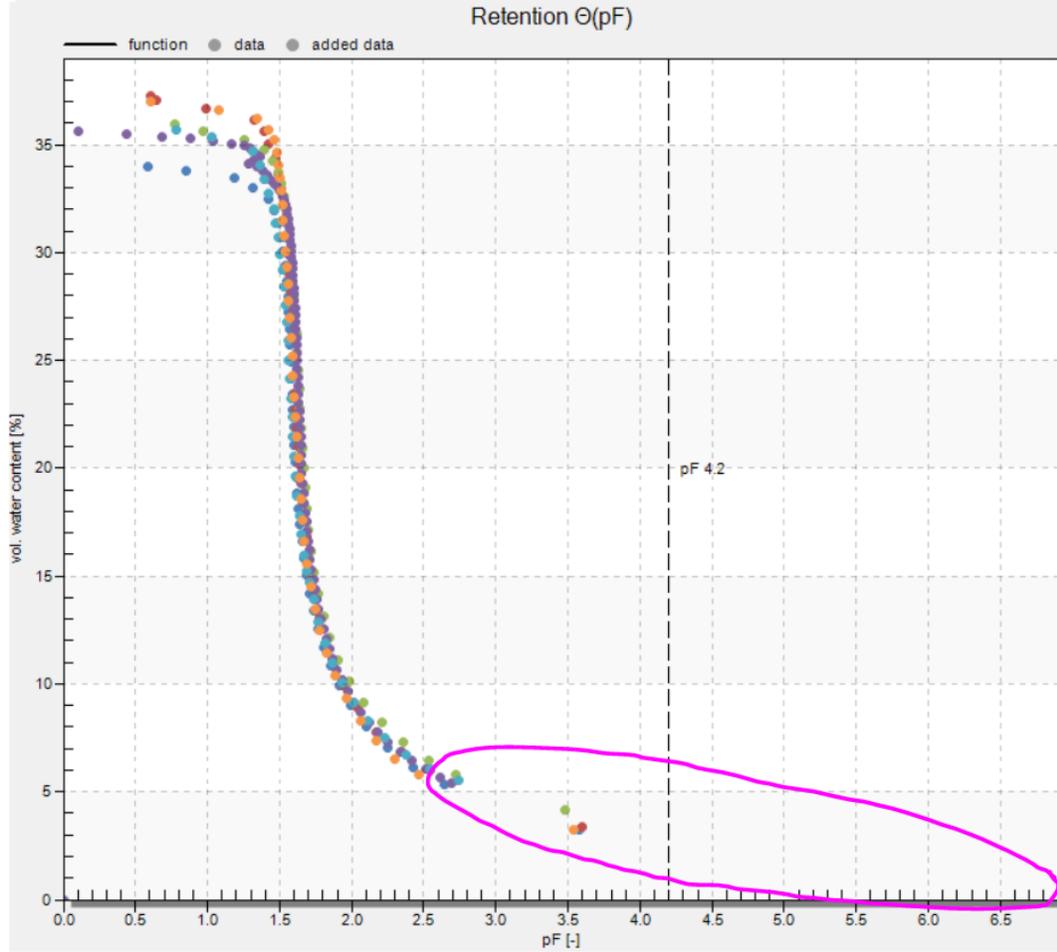
ESTIMATING THE SOIL MOISTURE RETENTION CHARACTERISTIC FROM TEXTURE, BULK-DENSITY, AND CARBON CONTENT

H VEREECKEN, J MAES, J FEYEN, P DARIUS
Soil Science 148 (6), 389-403

SHP from evaporation method

(HYRPOP, Soil Schunteraue, undisturbed cores, Boku Praktikum 2014, 6 independent replicates)

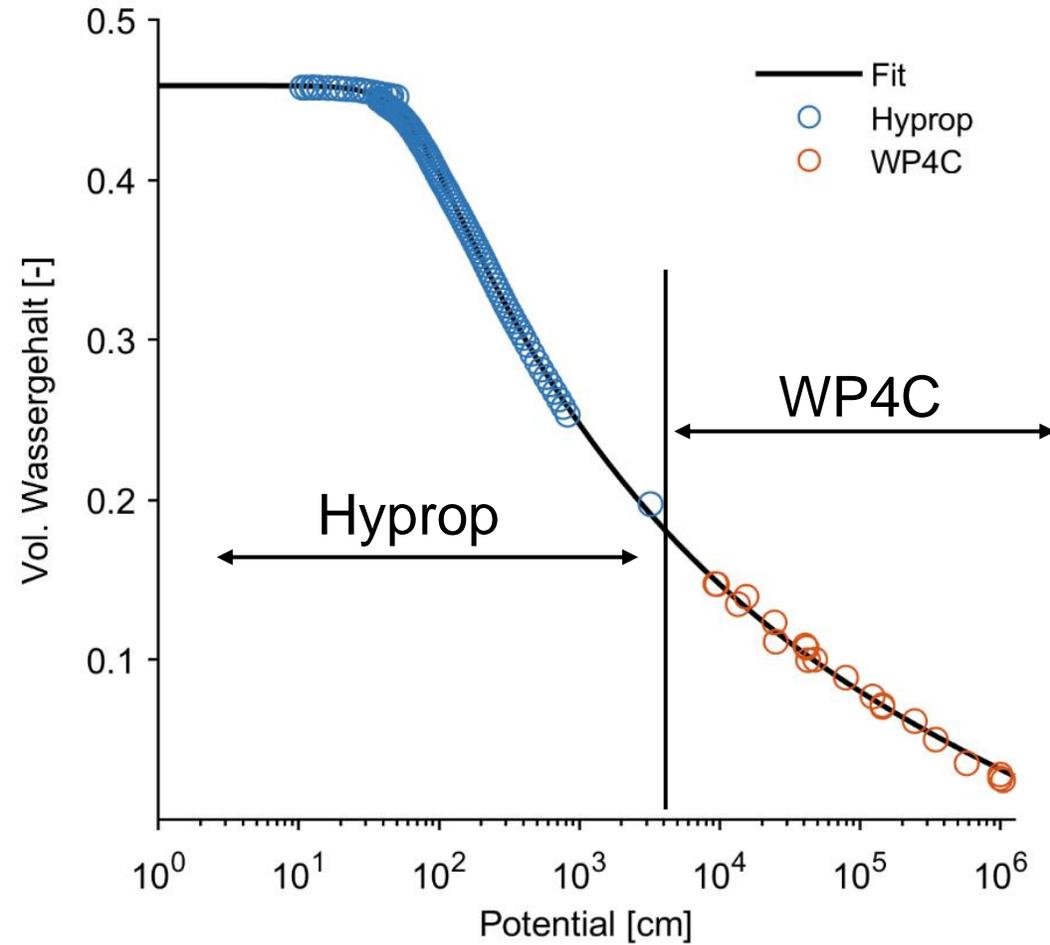




Dewpoint Potentiometer



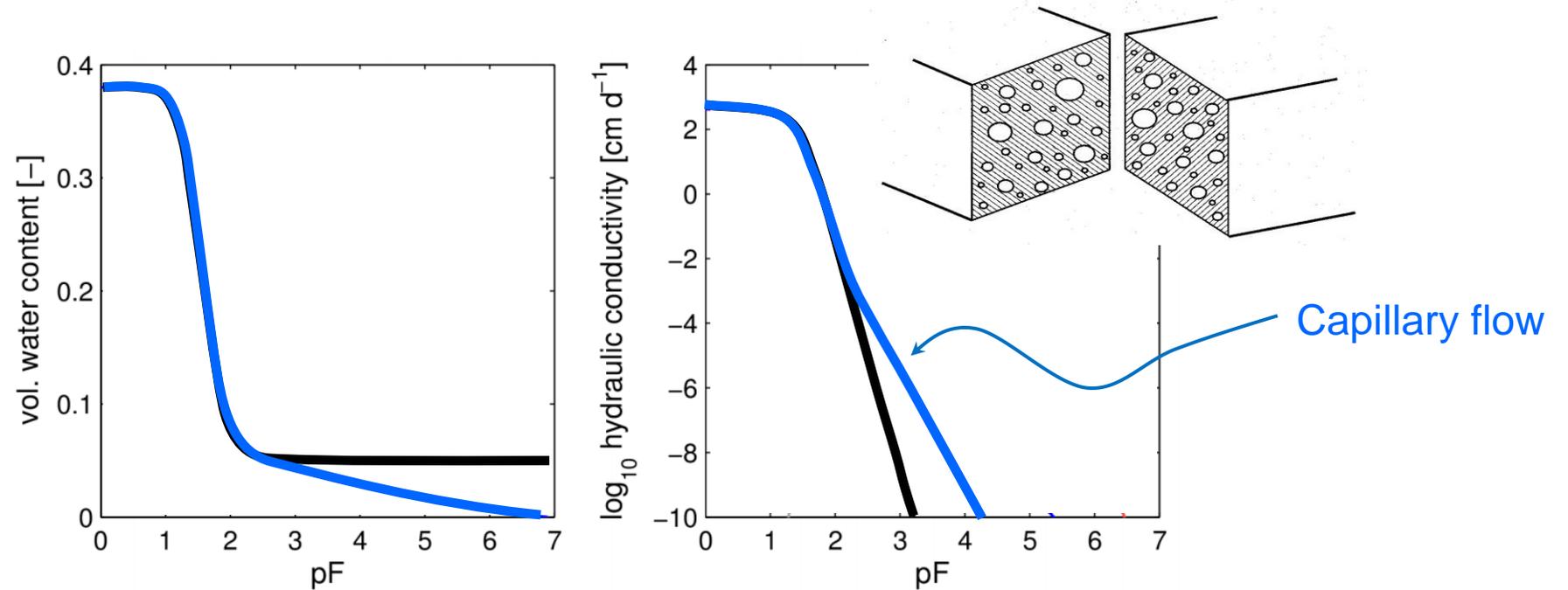
Messung der Retentionskurve



Lessons learned

Lessons learned (1)

better ...

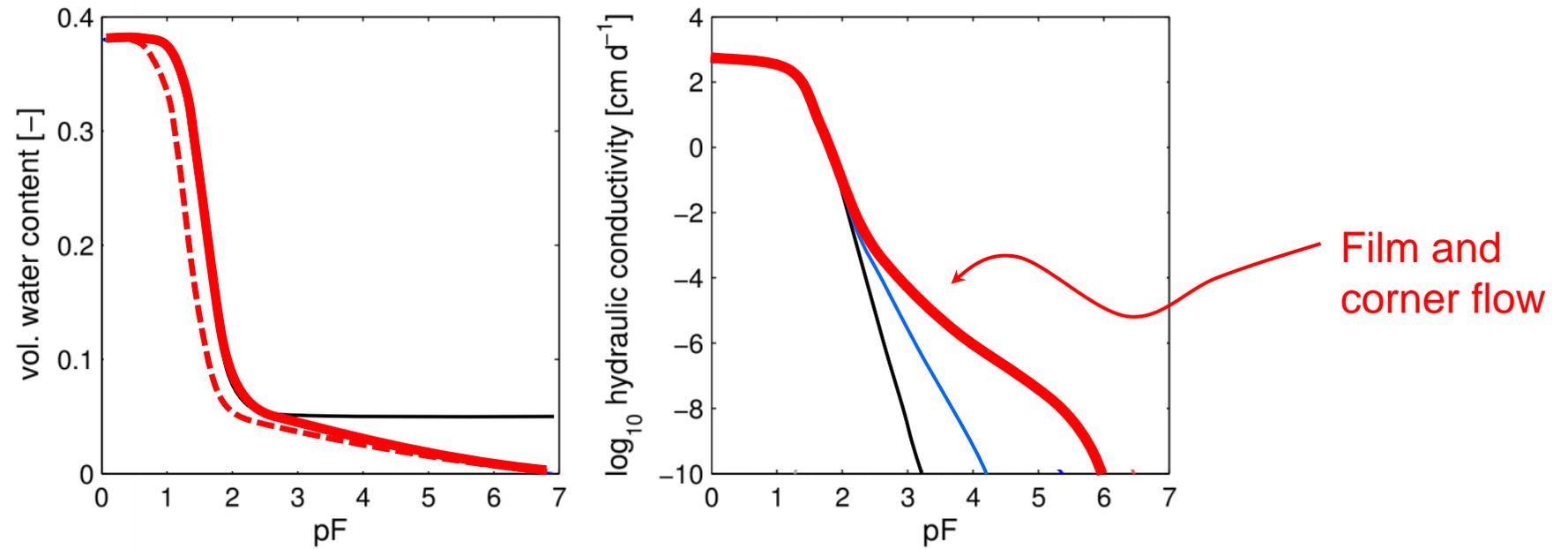


Ross et al. 1991 | Campbell-Shiozawa 1992 | Rossi and Nimmo 1994 | Fredlund-Xing 1994 | Fayer-Simmons 1995 | Morel-Seytoux and Nimmo 1999 | Webb 2002 | Groenevelt and Grant 2004 | Khlosi et al 2006 | ...



Lessons learned (2)

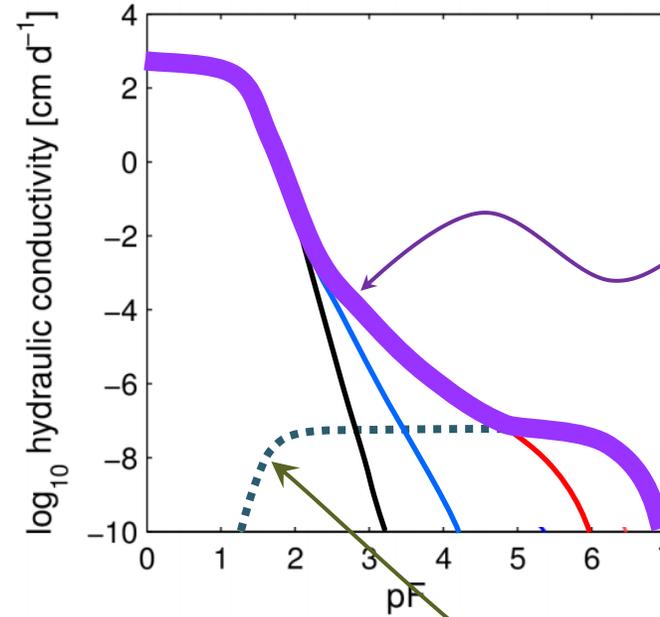
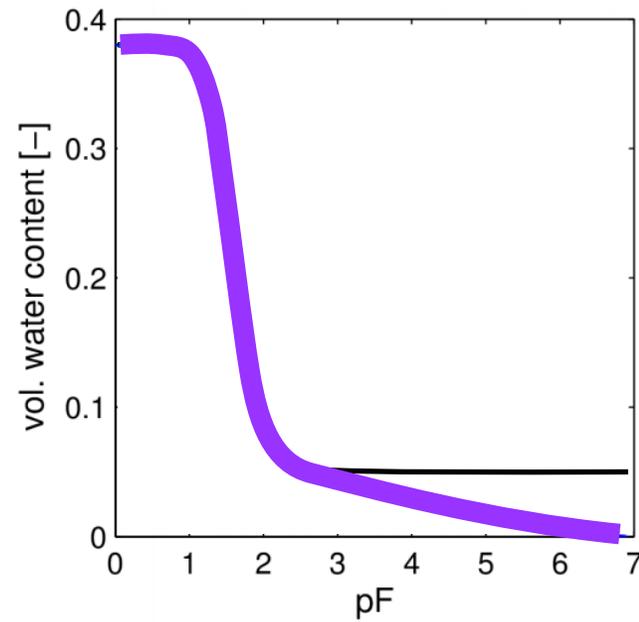
... even better ...



Tuller-Or 2001 | Peters-Durner 2008 | Tokunaga 2009 | Lebeau-Konrad 2010 | Zhang 2011 | Diamantopoulos-Durner, 2013 | ...

Lessons learned (3)

... really good !



Philip and de Vries 1957 | Saito et al. 2006

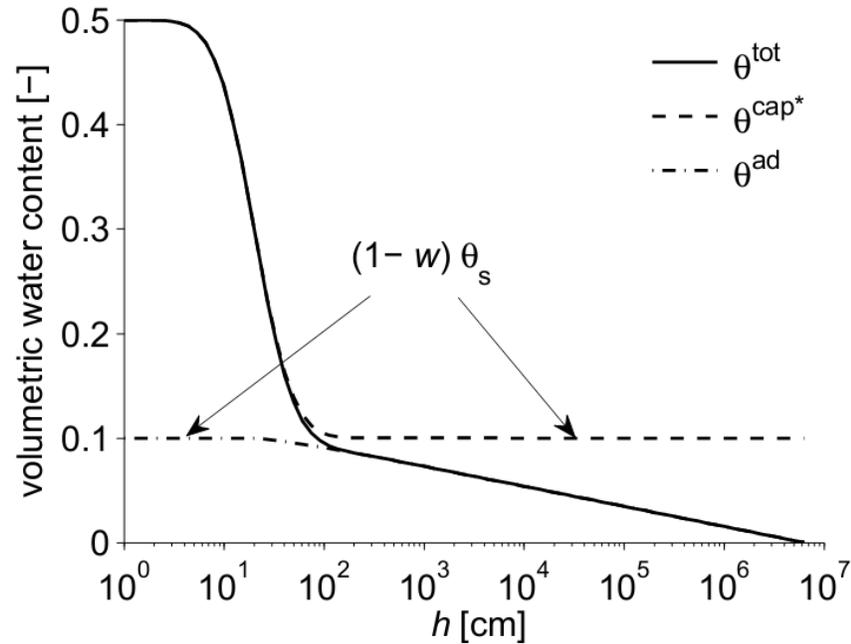
effective total conductivity

vapor flow component

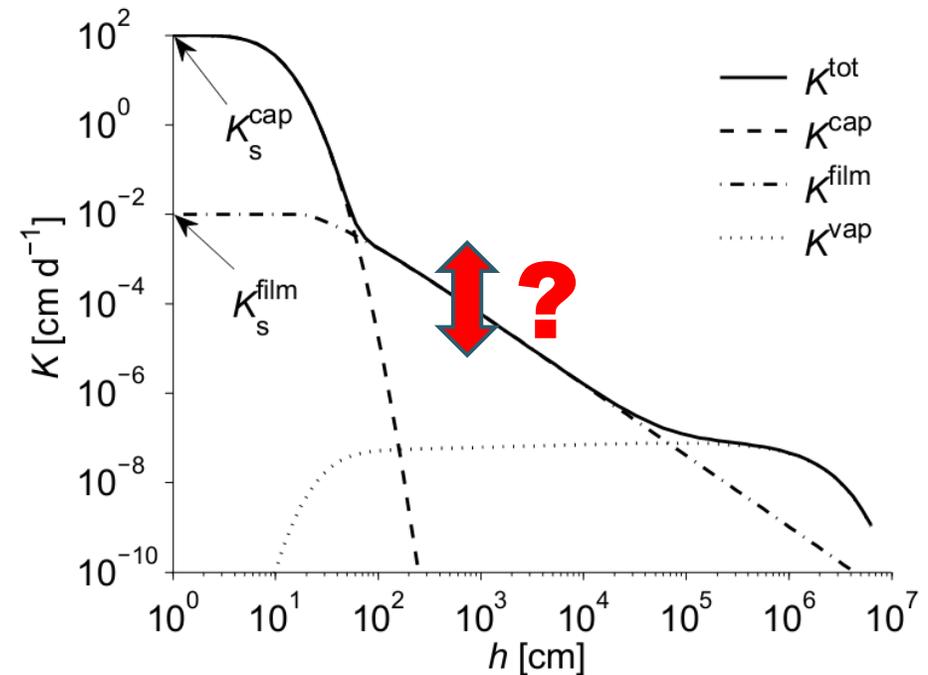


A parsimonious SHP description: The PDI model structure

$$\theta(h) = (\theta_s - \theta_r) S_{\text{cap}}(h) + \theta_r S_{\text{ad}}(h)$$



$$K^{\text{lv}} = K^{\text{liq}} + K^{\text{vap}} = K^{\text{cap}} + K^{\text{film}} + K^{\text{vap}}$$



The PDI model with K_{nc} prediction

Water Resources Research

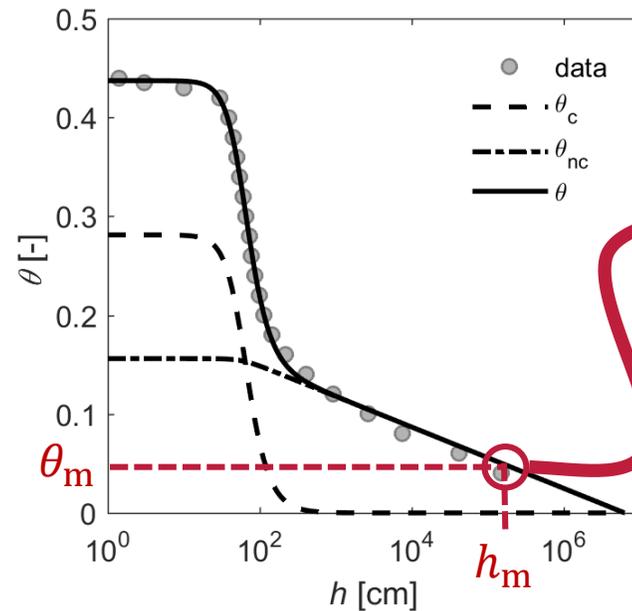
Research Article | [Open Access](#) |

A Simple Model to Predict Hydraulic Conductivity in Medium to Dry Soil From the Water Retention Curve

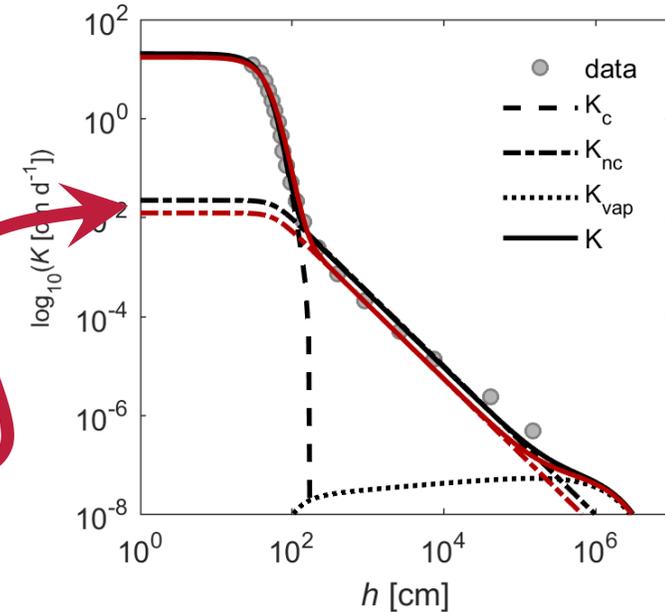
Andre Peters Tobias L. Hohenbrink, Sascha C. Iden, Wolfgang Durner

First published: 05 May 2021 | <https://doi.org/10.1029/2020WR029211>

Retention Model
4 parameters



Conductivity Model
2 parameters



$$K_{s,nc} = \theta_m c h_a^{-1.5}$$

$$c = \frac{2}{3} \frac{\pi^{7/3}}{\eta(\rho g)^{1/6}} \left(\frac{6}{A_{svl}}\right)^{1/3} \left(\frac{\epsilon_r \epsilon_0}{2}\right)^{3/2} \left(\frac{k_b T}{eZ}\right)^3 h_m^{1/3} \approx 98 \text{ cm}^{5/2} \text{ d}^{-1}$$

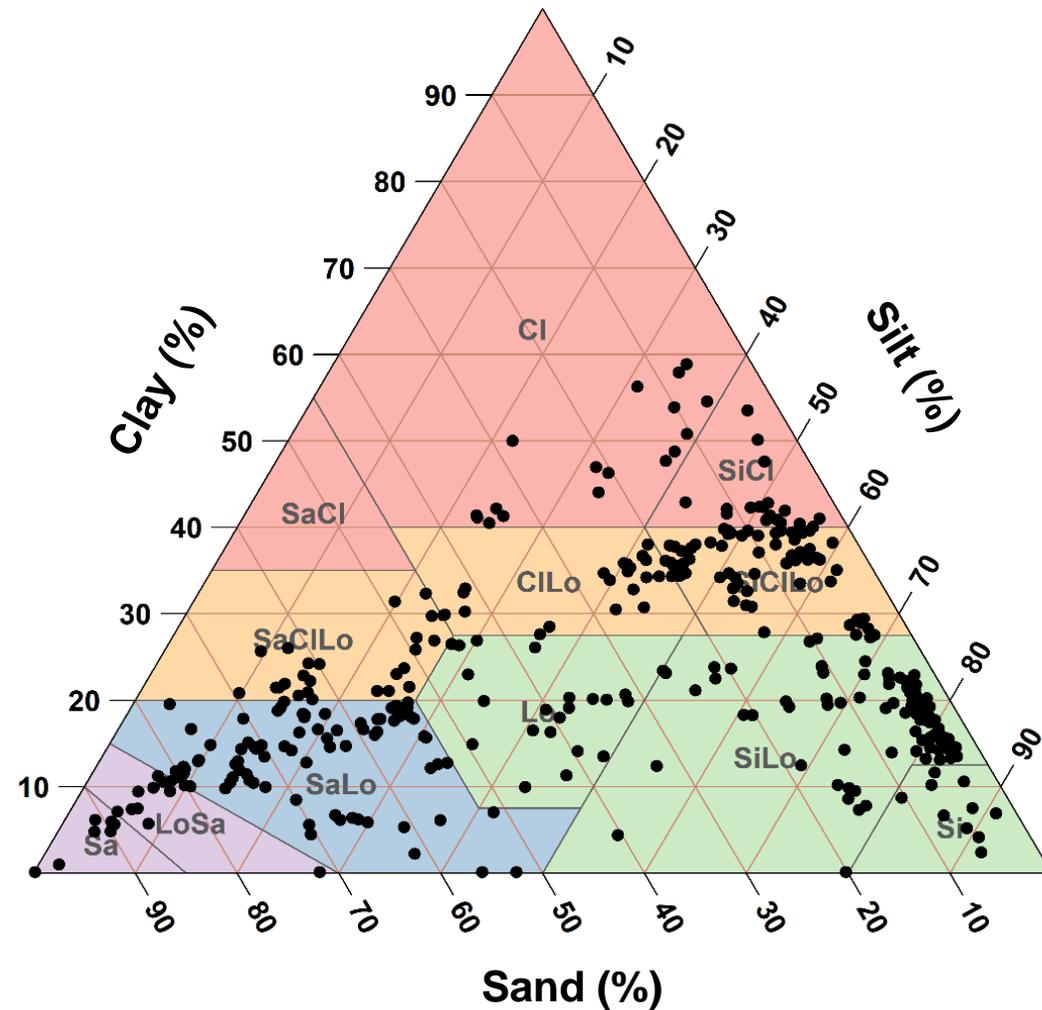


Test of the PDI k prediction



Model testing

- 484 **retention** and **conductivity** curves
- Determined on **undisturbed samples**
- Measured in the laboratory with:
 - **Evaporation method (HYPROP)**
 - **Dew point method (WP4C)**



Model combinations

Shape function:

- van Genuchten/Mualem, $m = 1 - 1/n$ **(VGM)**

Consideration of non-capillary water:

- No consideration **(orig VGM)**
- PDI model system with K_{nc} fitted **(PDI)**
- PDI model system with K_{nc} **predicted (PDlc)**

Fitted (green) and fixed (orange) parameters of the investigated model combinations.

	α (cm ⁻¹)	n (-)	θ_r (-)	θ_s (-)	m (-)	k_s (cm d ⁻¹)	τ (-)	c (cm ^{5/2} d ⁻¹)	Number of parameters
VGM - orig	✓	✓	✓	✓	1-1/n	✓	✓	-	6
VGM – PDI	✓	✓	✓	✓	1-1/n	✓	✓	✓	7
VGM – PDlc	✓	✓	✓	✓	1-1/n	✓	✓	98	6



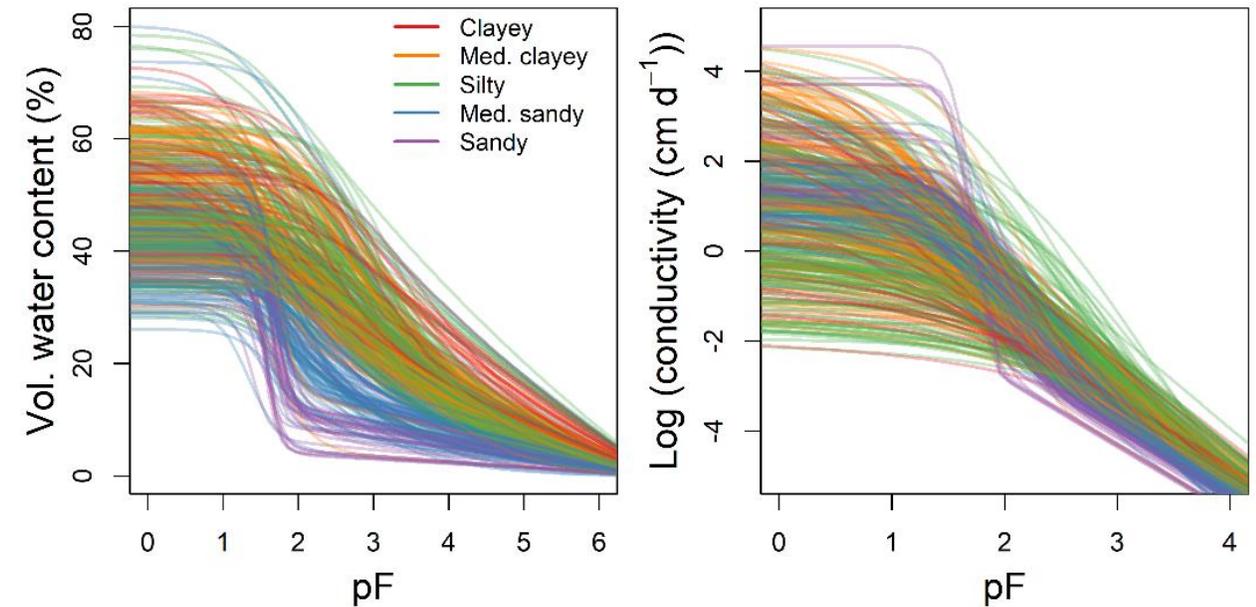
Estimation of model parameters

The **model combinations** were **fitted** to each **data set** from the data collection

Software: **SHYPFIT 2.0**

Algorithm: **Shuffled Complex Evolution**

Criterion: **Weighted Sums of Squares (WSSQ)**

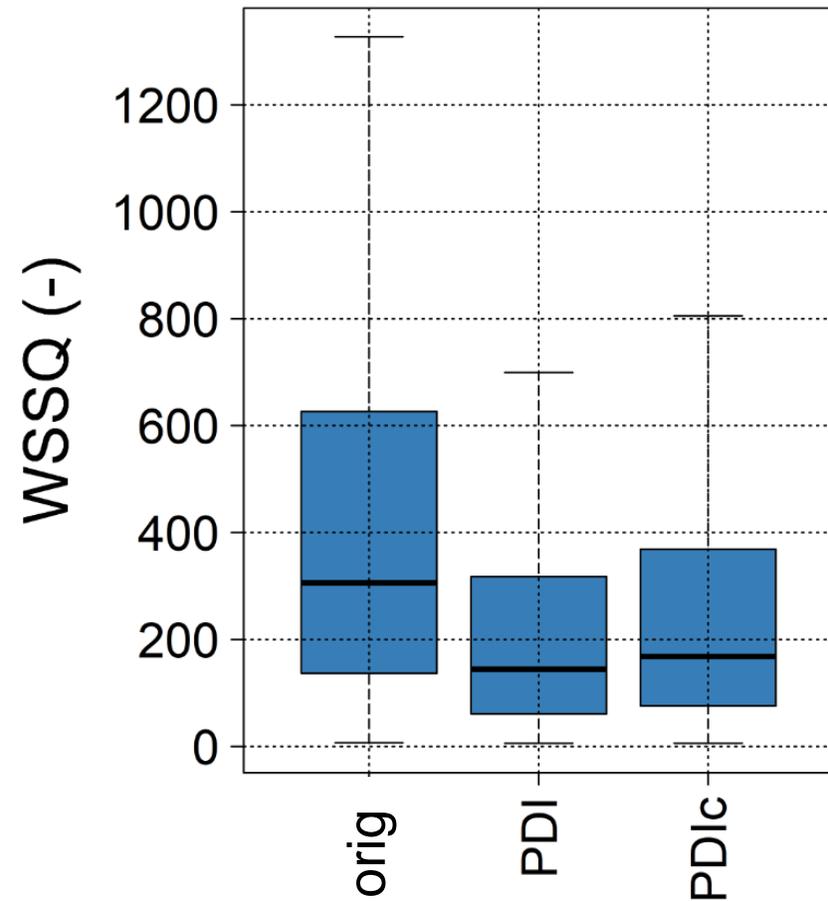


Soil water retention curves (left) and curves of hydraulic conductivity of the unsaturated soil (right) fitted for the VGM-PD1c model.

Overall model performance

WSSQ:

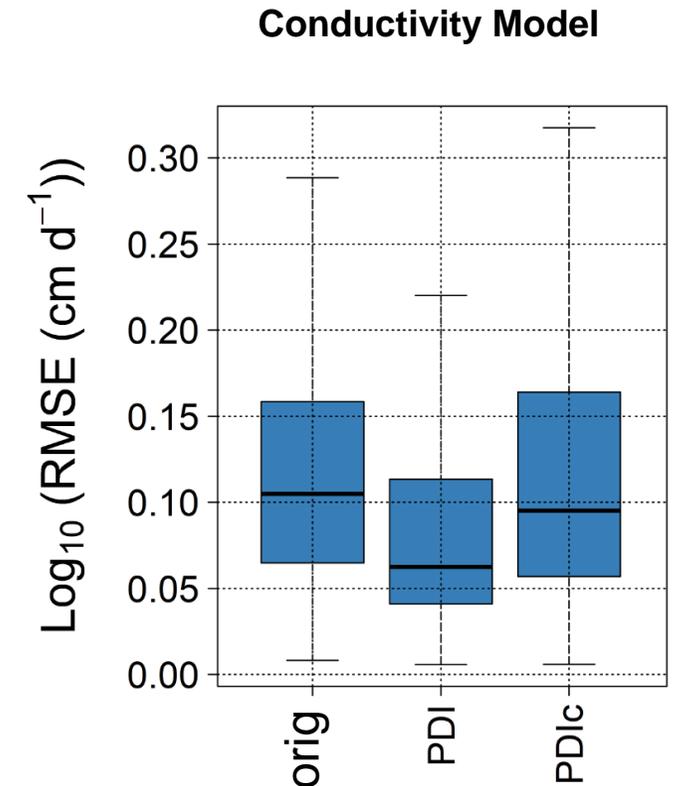
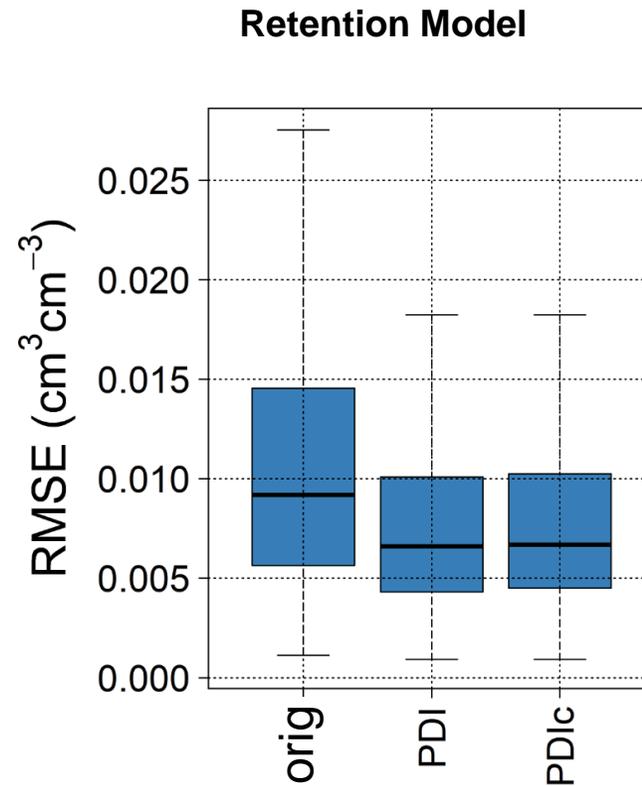
- PDI with and fitted and predicted K_{nc} perform similarly
- WSSQ by about 50 % reduced as compared to original VGM



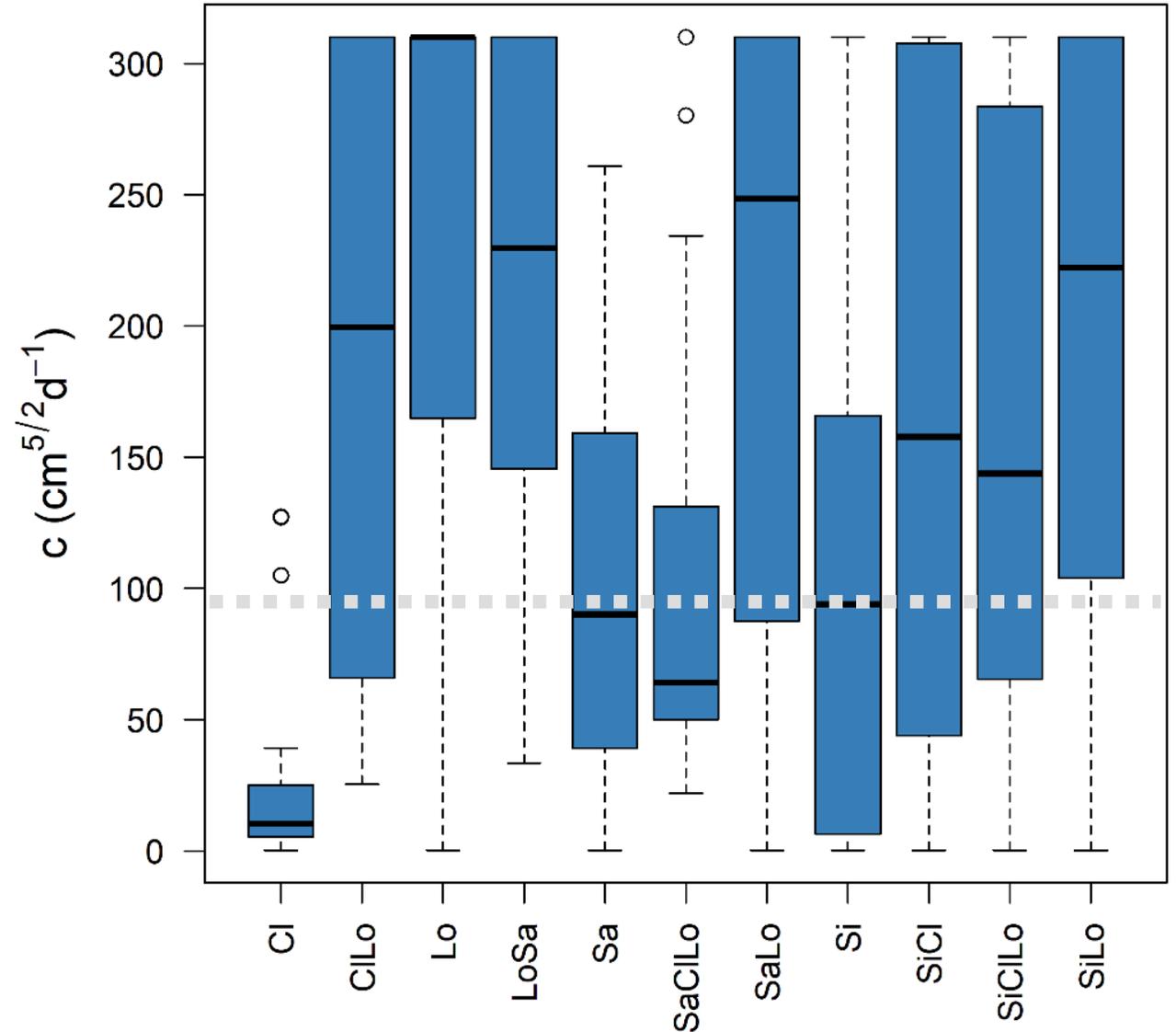
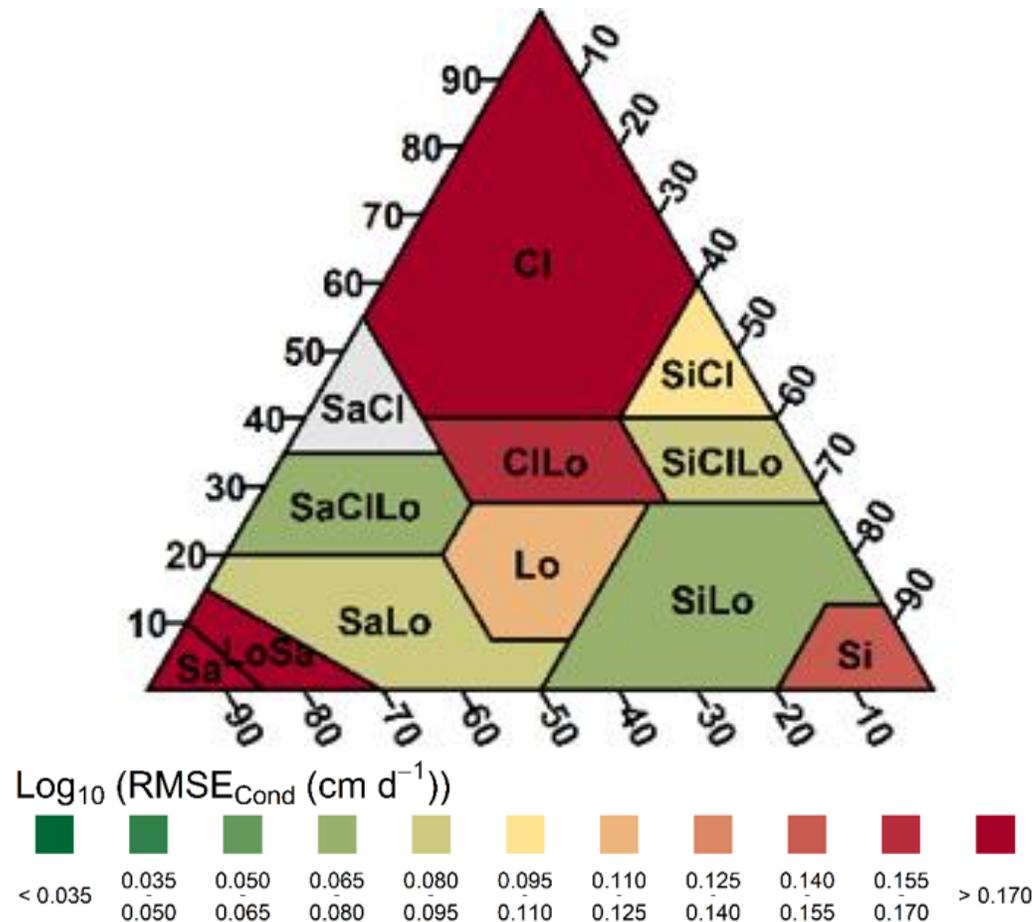
Model performance

Root mean Squared errors (RMSE):

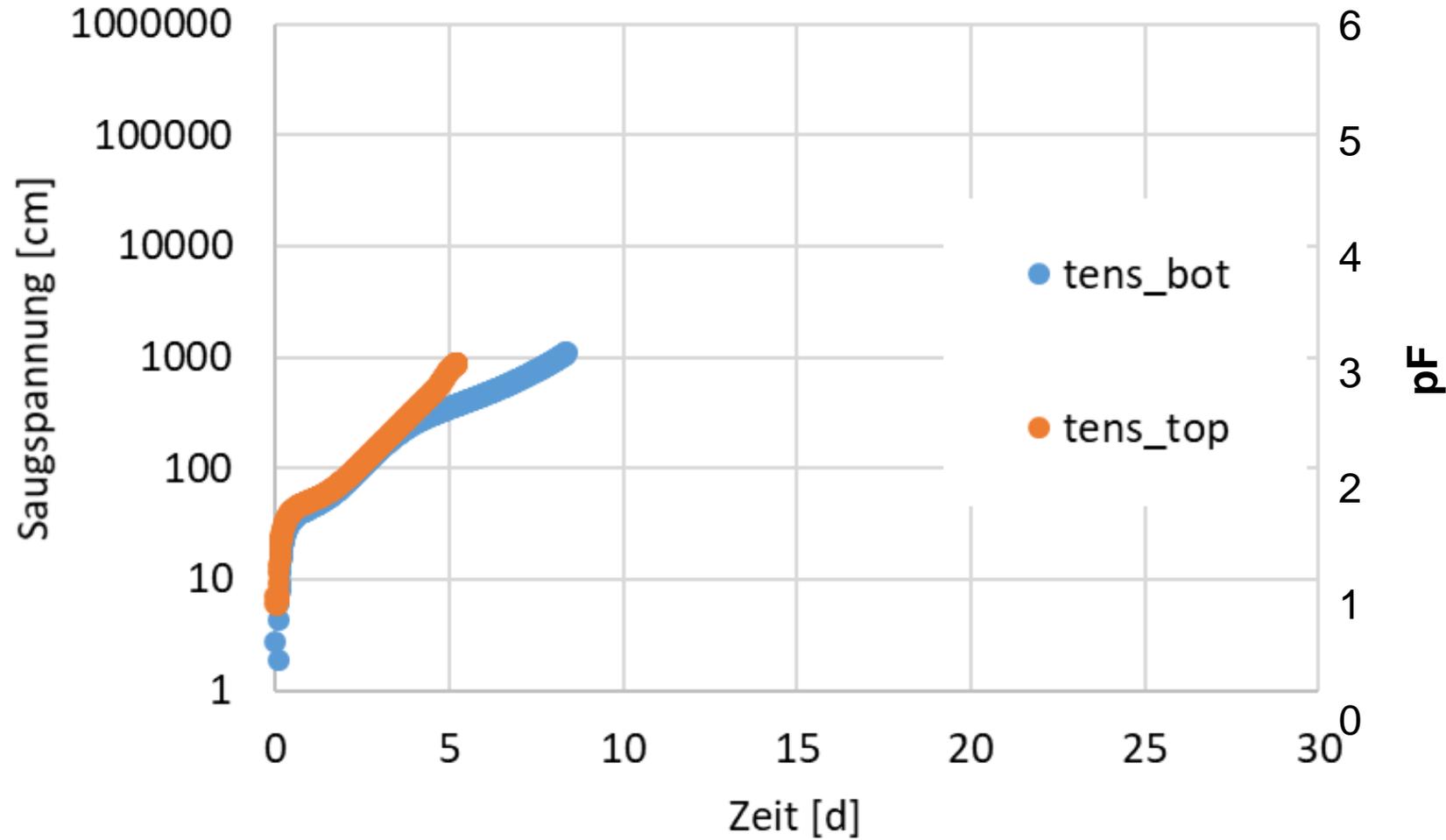
- Retention model: similar for **PDI** and **PDlc**
- Conductivity model: decrease in the order **orig** > **PDlc** > **PDI**

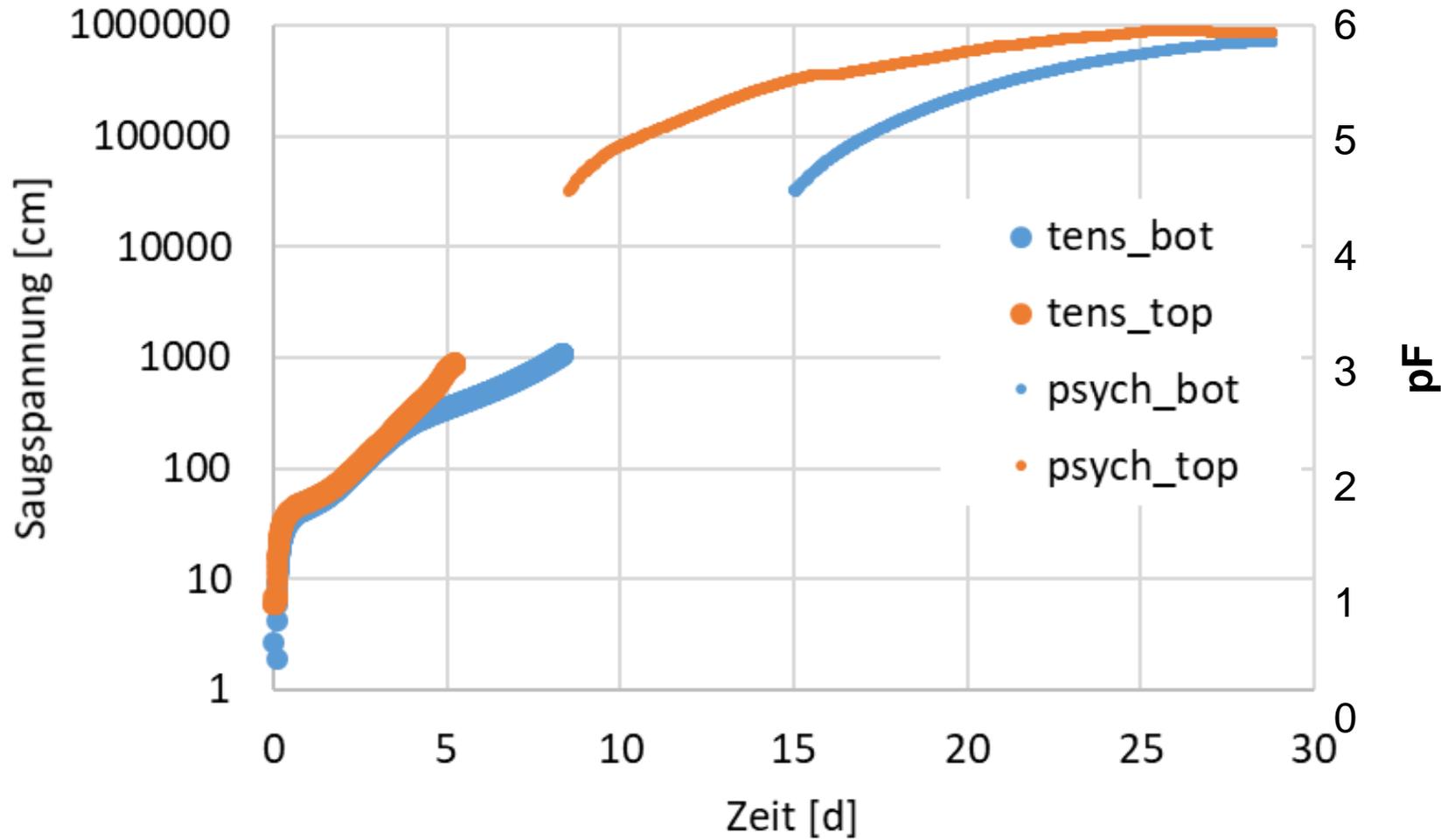


Is there a unique best „c“ for all soil texture classes?

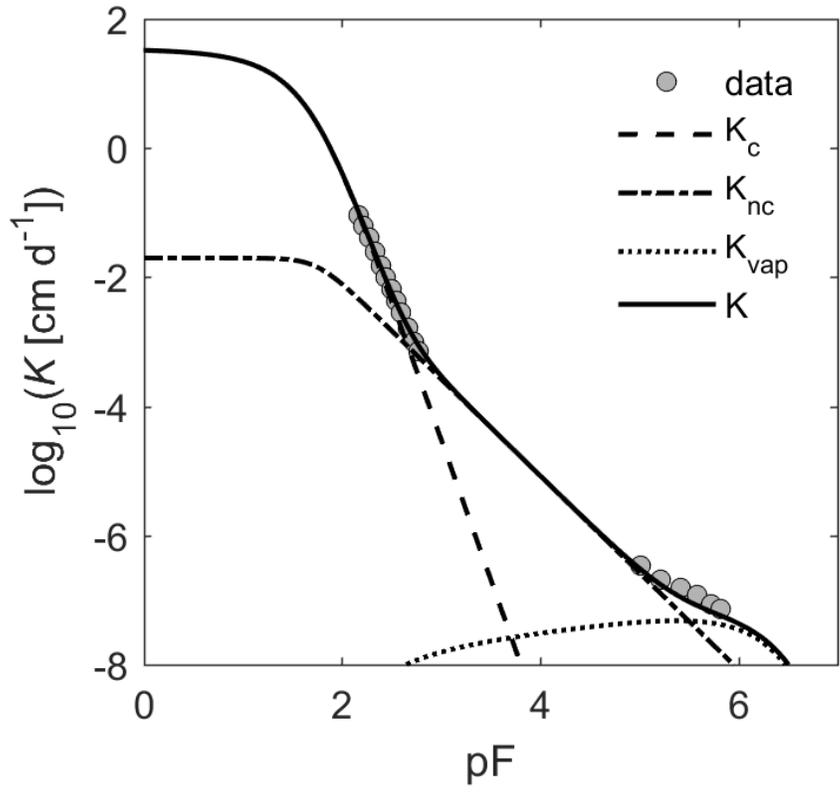
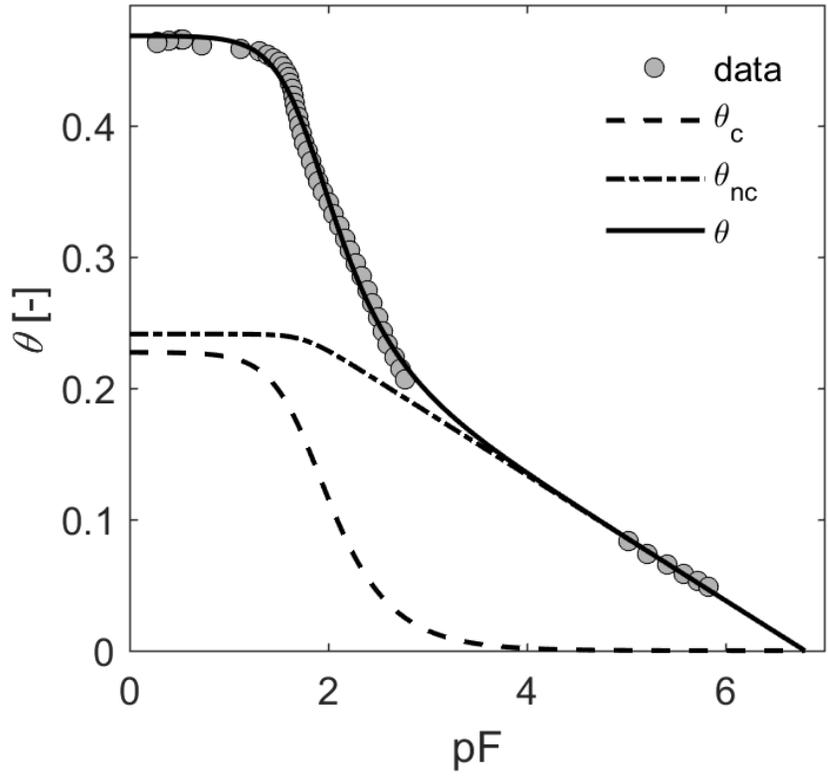


Outlook





range of
psychrometers:
pF 4.5 to pF 6



Range for
Psychrometers:
pF 4.5 to pF 6

p: 0.5 for
tensiometer
data and 0.1 for
psychrometer
data



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THANK
YOU ♡

